Practical aspects of $^1$H transverse paramagnetic relaxation enhancement measurements on macromolecules

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Abstract

The use of $^1$H transverse paramagnetic relaxation enhancement (PRE) has seen a resurgence in recent years as a method for providing long-range distance information for structural studies and as a probe of large amplitude motions and lowly populated transient intermediates in macromolecular association. In this paper we discuss various practical aspects pertaining to accurate measurement of PRE $^1$H transverse relaxation rates ($T_2$). We first show that accurate $T_2$ rates can be obtained from a two time-point measurement without requiring any fitting procedures or complicated error estimations, and no additional accuracy is achieved from multiple time-point measurements recorded in the same experiment time. Optimal setting of the two time-points that minimize experimental errors is also discussed. Next we show that the simplistic single time-point measurement that has been commonly used in the literature, can substantially underestimate the true value of $T_2$, unless a relatively long repetition delay is employed. We then examine the field dependence of $T_2$, and show that $T_2$ exhibits only a very weak field dependence at high magnetic fields typically employed in macromolecular studies. The theoretical basis for this observation is discussed. Finally, we investigate the impact of contamination of the paramagnetic sample by trace amounts ($\leq 5\%$) of the corresponding diamagnetic species on the accuracy of $T_2$ measurements. Errors in $T_2$ introduced by such diamagnetic contamination are potentially sizeable, but can be significantly reduced by using a relatively short time interval for the two time-point $T_2$ measurement.

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Keywords: $^1$H-$T_2$; Paramagnetic relaxation enhancement; EDTA-Mn$^{2+}$; Spin-label

1. Introduction

The history of paramagnetic relaxation enhancement (PRE) dates back to that of the nuclear Overhauser effect (NOE). Indeed, in Solomon’s classic 1955 paper, the relevant equations for both the NOE and PRE were presented [1]. Despite the long history of the PRE and its potential to provide unique long-range distance information in the 15–35 Å range, until relatively recently, applications of the PRE to studies of biological macromolecules that do not possess an intrinsic paramagnetic group, have been rather limited. Recent technical advances that permit easy and reliable conjugation of a paramagnetic group to a specific site have changed this situation, and PRE studies on macromolecules, to which an extrinsic paramagnetic group has been attached, are becoming increasingly popular.

The PRE arising from unpaired electrons with an isotropic $g$-tensor (such as a nitroxide spin-label or EDTA-Mn$^{2+}$) has proved to be a versatile tool. PRE analysis for such systems is simple, since there are no pseudo-contact shifts, and Curie-spin relaxation that could potentially exhibit significant cross-correlation with other relaxation mechanisms [2,3], is negligible. Using this type of PRE data, macromolecular structures have been characterized for soluble proteins [4–10], protein–protein complexes [11–14], protein–oligosaccharide complexes [15,16], protein–nucleic acid complexes [17–21], and membrane proteins [22,23]. The PRE can also provide information...
relating to large-scale dynamics that accompany changes of paramagnetic center—$^1$H distances, for example in non-specific protein–DNA interactions [24,25] and inter-domain motions [26]. A recent major advance in the field is the finding that in the fast exchange regime the intermolecular PRE can provide a powerful probe to detect and characterize transient, lowly populated intermediates in macromolecular binding events, thereby providing structural information on encounter complexes that cannot be obtained by any other biophysical technique [27,28].

For such investigations, the PRE for $^1$H-transverse magnetization (referred to here as $^1$H-$T_2$) is often used. The large magnitude of $^1$H-$T_2$ makes it a highly sensitive probe. This is due to the large nuclear gyromagnetic ratio of the proton and the primary dependence of $^1$H-$T_2$ on the spectral density function at zero-frequency. In addition, $^1$H-$T_2$ is much less susceptible to internal motions and cross relaxation than the longitudinal $^1$H-PRE (referred to as $^1$H-$T_1$) which is highly sensitive to these two factors [20]. For quantitative analysis, it is very important to accurately and precisely measure $^1$H-$T_2$ rates and to understand potential pitfalls in the measurements. In this paper, we describe practical aspects of $^1$H-$T_2$ measurements for amide protons of proteins.

2. Materials and methods

2.1. NMR samples

Experimental PRE data were acquired on two samples: a 20 kDa complex between $^2$H/$^15$N-labeled SRY and a 14-bp DNA duplex with $d$T-EDTA located at the third base-pair (site c displayed in Fig. 2 of Ref. [20]); and $^15$N-labeled HPr(E32C) with EDTA-Mn$^{2+}$ conjugated at Cys32.

Expression and purification of SRY was carried out as described by Murphy et al. [29]. Samples of the complexes chelating Mn$^{2+}$ or Ca$^{2+}$ were prepared as described [19,20]. Data were recorded on 0.3 mM complex dissolved in 10 mM Tris–HCl (pH 7.4), 20 mM NaCl, and 7% D$_2$O.

Expression and purification of HPr(E32C) and the conjugation reaction with N-[S-(2-pyridylthio)cysteaminyl]ethylenediamine-Ν,Ν',Ν''-tetraacetic acid (Toronto Research Chemicals) were carried out as described [28]. The final conjugated HPr(E32C)–EDTA-Mn$^{2+}$ or –EDTA-Ca$^{2+}$ samples were further purified by Mono-Q anion-exchange chromatography. NMR data on the paramagnetic (Mn$^{2+}$) and diamagnetic (Ca$^{2+}$) states were recorded using 0.3 mM protein dissolved in 10 mM Tris–HCl (pH 7.4), and 5% D$_2$O.

The chemical shifts for the Mn$^{2+}$ and Ca$^{2+}$-chelated states of the SRY/DNA complex are identical, indicating that pseudo-contact shifts are negligible and, therefore, the electronic $g$-tensor for the unpaired electrons of Mn$^{2+}$ is indeed isotropic. An isotropic $g$-tensor for the unpaired electrons of Mn$^{2+}$ in EDTA-Mn$^{2+}$ conjugated to either DNA or protein was also found in previous studies, including systems ranging from 20 to 50 kDa [10,19,23–28].

2.2. NMR measurements

Measurements of PRE $^1$H-$T_2$ rates were carried out using Bruker DMX-500, DRX-600, and DRX-800 spectrometers equipped with z-gradient triple resonance cryogenic probes. Identical $T_2$ experiments were performed on two samples, one with Mn$^{2+}$ (paramagnetic) conjugated to EDTA and the other with Ca$^{2+}$ (diamagnetic). The $^1$H-$T_2$ rates are given by the difference in $^1$H-$R_2$ rates between the paramagnetic and diamagnetic samples. For PRE applications, we found that conventional NMR tubes were better in terms of shimming than Shigemi microtubes, presumably because the magnetic susceptibility of the paramagnetic sample is quite different from that for a micro-cell matched for H$_2$O-based diamagnetic samples. The pulse sequence employed is given in Fig. 1. $^1$H-$T_2$ measurements with multiple time-points were carried out in an interleaved manner. The recorded data were processed with the NMRPipe software [30]. Shifted cosine bell window-functions were applied to both the $^1$H and $^15$N time-domains, followed by zero-filling and Fourier transformation.

(Note, we found that the type of window-function employed does not affect the $R_2$ values obtained from multiple-time-point measurements). For the single-time-point approach, which requires Lorentzian line-shapes in the $^1$H dimension, an exponential window-function was applied instead. Peak heights were quantified with either the NMRView [31] or NMRDraw [30] software. PRE $^1$H-$T_2$ rates were determined from the peak heights for diamagnetic and paramagnetic samples ($I_{\text{dia}}$ and $I_{\text{para}}$, respectively) as a function of the delay $T$ (see Fig. 1) given by:

$$I_{\text{dia}}(T) = I_{\text{dia}}(0) \exp(-R_{2,\text{dia}} T)$$

$$I_{\text{para}}(T) = I_{\text{para}}(0) \exp(-(R_{2,\text{dia}} + R_2) T)$$

For two-time-point measurements, errors in $R_2$ were estimated as described in Section 3. Otherwise, errors were estimated using a Monte-Carlo approach.

3. Results and discussion

3.1. Experiment for $R_2$ measurements

At high magnetic fields ($^1$H frequency $\geq$500 MHz), the PRE rate, $R_2$, arising from the dipole–dipole interaction between a nucleus and unpaired electrons with an isotropic $g$-tensor is given by [1,32]

$$R_2 = \frac{1}{15} \left( \frac{\mu_0}{4\pi} \right)^2 g^2 \mu_0^2 S(S + 1) r^{-6} \left( 4\tau_e + \frac{3\tau_e}{1 + (\omega_H \tau_e)^2} \right)$$

where $r$ is the distance between the paramagnetic center and the observed nucleus; $\mu_0$, the permeability of vacuum; $g$, the electron $g$-factor;

μ_B, the electron Bohr magneton; S, the electron spin quantum number; τ_c, the PRE correlation time defined as τ^{-1}_c = τ^{-1}_r + τ^{-1}_α; τ_r, the rotational correlation time; τ_e, the electron relaxation time; and ω_{1H}/2π, the nuclear Larmor frequency. Although Eq. (3) is valid only for a system where the paramagnetic group is fixed within the molecular frame, the equation can be readily modified to deal with a system where the paramagnetic center is mobile as described in our previous paper [20].

In practice, \( \Gamma_2 \) is measured as a difference in transverse relaxation rates between the paramagnetic \( \langle R_{2,\text{para}} \rangle \) and diamagnetic \( \langle R_{2,\text{dia}} \rangle \) states

\[
\Gamma_2 = \langle R_{2,\text{para}} \rangle - \langle R_{2,\text{dia}} \rangle
\]

This subtraction cancels out all relaxation mechanisms common to both states, including exchange contributions to the transverse relaxation rate \( R_2 \), such that the only remaining relaxation mechanism arises from electron–nucleus interactions. Fig. 1 shows the pulse sequence we have been using for \( ^1H-\Gamma_2 \) measurements [19,23–25,27], which is essentially the same as that proposed by Kay and co-workers [8]. The period for the \( ^1H \) transverse relaxation measurement is incorporated in the first INEPT scheme. During the \( ^1H \) transverse period of \( T + 2\tau_{in}, \) \( ^15N \) 180 pulses swap the slow and fast relaxing components (represented by \( H_x - 2H_yN_z \) and \( H_t + 2H_yN_z \), respectively) and the contributions from the two components are identical, making the overall decay a single-exponential process with an average relaxation rate. The observed relaxation rates correspond to \( 1/T_2 \) for \( ^1H \) in-phase terms, since the transverse relaxation rates for \( H_y \) and \( 2H_yN_z \) terms are expected to be virtually identical for macromolecules. (Note that \( T_1 \) relaxation of \( N_z \) is much slower than \( ^1H \ T_2 \).) Identical experiments are performed for the paramagnetic and diamagnetic samples to obtain \( \Delta \Gamma_2 \).

### 3.2. Two-time-point experiment for measurement of \( \Gamma_2 \) rates

A two-time-point measurement provides a simple means of obtaining \( \Gamma_2 \) rates and their corresponding errors without making use of any fitting procedures. In this approach, \( ^1H-\Gamma_2 \) rates are determined from two time points \( (T = 0 \text{ and } \Delta T) \) for transverse relaxation using Eqs. (1) and (2) as follows:

\[
\Gamma_2 = \frac{1}{T_b - T_a} \ln \frac{I_{\text{dia}}(T_a)I_{\text{para}}(T_b)}{I_{\text{dia}}(T_b)I_{\text{para}}(T_a)}
\]

where \( I_{\text{dia}} \) and \( I_{\text{para}} \) are the peak intensities for the diamagnetic and paramagnetic states, respectively. It should be noted that effects of homonuclear \( ^3J_{\text{HNH}} \)-modulation during \( T \) are cancelled out by using identical times and taking ratios for the two states. The errors in \( \Gamma_2 \) can be propagated from Eq. (5) and are given by

\[
\sigma(\Gamma_2) = \frac{1}{T_b - T_a} \times \sqrt{\frac{\sigma_{\text{dia}}}{I_{\text{dia}}(T_a)} + \frac{\sigma_{\text{dia}}}{I_{\text{dia}}(T_b)} + \frac{\sigma_{\text{para}}}{I_{\text{para}}(T_a)} + \frac{\sigma_{\text{para}}}{I_{\text{para}}(T_b)}}
\]

where \( \sigma_{\text{dia}} \) and \( \sigma_{\text{para}} \) are the standard deviations of the noise in the spectra recorded for the diamagnetic and paramagnetic states, respectively.

The two time-points should be chosen to minimize the errors in the \( \Gamma_2 \) rates. Fig. 2 illustrates the theoretical relationship between \( \Delta T \) and the error in \( \Gamma_2 \), obtained using Eqs. (1), (2), and (6) together with the following equation:
where $\tau$ represents the overall $^1$H transverse period for the coherence transfers (9.9 ms). Eq. (7) assumes a Lorentzian line-shape in the $^1$H-dimension, equal recovery levels during the repetition delay, and the same concentration and number of scans for both the diamagnetic and paramagnetic samples. Under these conditions, the error $\sigma(I_2)$ is minimal when $T_a = 0$ and $T_b \approx 1.15/(R_{2,\text{dia}} + \Gamma_2)$. As can be seen from Fig. 2, the larger the value of $\Gamma_2$, the narrower the optimal range of $T$. Therefore, the second time-point should be set to be optimal for a relatively large $\Gamma_2$ expected for the system under study. For example, if the range of expected $\Gamma_2$ rates is $0$–75 $s^{-1}$, a second time-point at $\approx 1.15/(R_{2,\text{dia}} + \Gamma_2)$ represents a reasonable choice. (However, if diamagnetic contamination in the paramagnetic sample is greater than $\sim 3\%$, smaller values are required for accurate measurement of intramolecular $\Gamma_2$ rates; see below).

To obtain reasonably precise data with errors smaller than $\sim 10\%$ for $\Gamma_2$ rates of $\sim 50$ $s^{-1}$, the number of accumulated scans per FID should typically be set to at least 32 for measurements using a cryogenic probe on a $^1$H-dimension, equal recovery levels during the repetition delay, and the same concentration and number of scans for both the diamagnetic and paramagnetic samples. Under these circumstances, the total length of data collection is proportional to the number of time-points. For each simulation, the noise standard deviation $\sigma_I$ was set to 0.5% of $I_{\text{dia}}(0)$ in Eq. (1). The relaxation rate for the diamagnetic state was set to 50 $s^{-1}$ and four values of the true $\Gamma_2$ (10, 25, 50, and 75 $s^{-1}$) were examined. As Table 1 shows, increasing the number of time-points without sacrificing the number of accumulated scans does indeed improve the precision in the $\Gamma_2$ measurement. (Note in these calculations with synthetic data, precision and accuracy are equivalent).

In practice, however, spectrometer access may be limited, in which case increasing the number of time-points would entail a proportionate decrease in the number of accumulated scans per time-point to keep the total measurement time the same. Interesting questions arise in this regard. Should one use many time-points sacrificing signal-to-noise (S/N) ratios for individual spectra? Or should one acquire high S/N ratio data with fewer time-points? To examine this issue, we carried out a second set of Monte-Carlo simulations in which the number of accumulated scans per time-point was assumed to be inversely proportional to the number of time-points ($n$), making the overall experiment length constant and $I_{\text{dia}}(0)/\sigma_I$ inversely proportional to $\sqrt{n}$. Table 2 shows the results of simulations using different $I_{\text{dia}}(0)/\sigma_I$ ratios but in other respects identical to the simulations reported in Table 1. Under these conditions, the simulations reveal that increasing the number points on the accuracy and precision of $\Gamma_2$ measurements using a Monte-Carlo approach. One hundred sets of synthetic data with random Gaussian noise were generated using Eqs. (1), (2), and (7). Non-linear least-squares fitting was then carried out for each dataset to obtain the standard deviation of the apparent $\Gamma_2$ values. The results for 2, 4, 8, and 16 time-points were compared.

First, we simulated the case where the same number of accumulated scans is employed per time-point (Table 1). Under these circumstances, the total length of data collection is proportional to the number of time-points. For each simulation, the noise standard deviation $\sigma_I$ was set to 0.5% of $I_{\text{dia}}(0)$ in Eq. (1). The relaxation rate for the diamagnetic state was set to 50 $s^{-1}$ and four values of the true $\Gamma_2$ (10, 25, 50, and 75 $s^{-1}$) were examined. As Table 1 shows, increasing the number of time-points without sacrificing the number of accumulated scans does indeed improve the precision in the $\Gamma_2$ measurement. (Note in these calculations with synthetic data, precision and accuracy are equivalent).

3.3. Impact of increasing the number of time-points on the accuracy of $\Gamma_2$ rates

Since one might expect that a large number of time-points may yield superior quality $\Gamma_2$ data, we investigated the impact of increasing the number of acquired time-points on the accuracy and precision of $\Gamma_2$ measurements using a Monte-Carlo approach. One hundred sets of synthetic data with random Gaussian noise were generated using Eqs. (1), (2), and (7). Non-linear least-squares fitting was then carried out for each dataset to obtain the standard deviation of the apparent $\Gamma_2$ values. The results for 2, 4, 8, and 16 time-points were compared.

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of time-points at a cost of a lower S/N ratio results in no gain in $I_2$ precision. Therefore, a two-time-point $I_2$ measurement with high S/N ratio represents a good choice in practice, since it requires neither fitting procedures nor complicated error estimations. This conclusion is confirmed experimentally by the excellent correlation between the measured $I_2$ rates for the SRY–DNA complex using 2 and 8 time-points (Fig. 3).

### 3.4. Inaccuracies of the single-time-point approach for the measurement of $I_2$ rates

Many studies in the literature have made use of a very simplistic approach in which only two regular HSQC spectra, one of the diamagnetic state and the other of the paramagnetic state at the same concentration, are employed to determine $^1H_N-I_2$ rates using Eq. (7). We refer to this method as the single-time-point approach. Eq. (7), however, only holds true if the repetition delay is sufficiently long to ensure that magnetization recovery levels are identical for the diamagnetic and paramagnetic states. However, for conventional HSQC experiments on biological macromolecules, the repetition delay between the scans is generally set to 0.8–2.0 s, which is not sufficient for 100% recovery of $^1H$ longitudinal magnetizations. Indeed, for a $^2H$-labeled protein, the amide $^1H-T_1$ relaxation time at regular magnetic fields ($^1H$ frequency of 500–800 MHz) is very long and a repetition delay longer than ~20 s would be required to achieve 100% recovery for all amide $^1H$ nuclei.

### Table 1

Impact of increasing time-points without reducing scan-accumulations on the precision of $I_2$ measurements

<table>
<thead>
<tr>
<th>$n$</th>
<th>$I_{dia(0)}/\sigma_I$</th>
<th>$\Delta T$</th>
<th>$R_{2, dia} = 50$ s$^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>$I_2 = 10$ s$^{-1}$</td>
</tr>
<tr>
<td>2</td>
<td>200</td>
<td>0.012</td>
<td>1.54</td>
</tr>
<tr>
<td>4</td>
<td>200</td>
<td>0.004</td>
<td>1.33</td>
</tr>
<tr>
<td>8</td>
<td>200</td>
<td>0.002</td>
<td>0.99</td>
</tr>
<tr>
<td>16</td>
<td>200</td>
<td>0.001</td>
<td>0.71</td>
</tr>
</tbody>
</table>

*a Calculations were carried out using a Monte-Carlo approach with 100 synthetic datasets as described in the main text. Definitions of symbols are as follows: $n$, number of time-points; $I_{dia(0)}$, peak intensity at $T = 0$ for the diamagnetic state; $\sigma_I$, noise standard deviation; $\Delta T$, interval for linear sampling of $T$ between 0 and $(n-1)\Delta T$; $\sigma(I_2)$, standard deviation of calculated $I_2$. The deviation of the calculated $I_2$ from the true $I_2$ was found to be almost same as $\sigma(I_2)$. Thus, for these calculations, precision and accuracy are essentially equivalent.

### Table 2

Impact of increasing time-points with reduced scan-accumulations, keeping the overall measurement time constant, on the precision of $I_2$ measurements

<table>
<thead>
<tr>
<th>$N$</th>
<th>$I_{dia(0)}/\sigma_I$</th>
<th>$\Delta T$</th>
<th>$R_{2, dia} = 50$ s$^{-1}$</th>
</tr>
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<tr>
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<td>200</td>
<td>0.004</td>
<td>1.33</td>
</tr>
<tr>
<td>8</td>
<td>100</td>
<td>0.002</td>
<td>0.98</td>
</tr>
<tr>
<td>16</td>
<td>71</td>
<td>0.001</td>
<td>0.71</td>
</tr>
</tbody>
</table>

*a Calculations were carried out in the same manner as for those in Table 1, except that different values of $I_{dia(0)}/\sigma_I$ were employed to simulate a constant overall measurement time in all cases. For example, to acquire 8 points for $T$, the number of scans should be a fourth of that for a 2 time-point measurement, resulting in a reduction of 2 in S/N ratio. Definitions of symbols are as given in Table 1.

![Fig. 3. Correlation between experimentally determined $^1H_N-I_2$ rates derived from two ($\Delta T = 14$ ms) and 8 time-point ($\Delta T = 2.8$ ms) measurements for the $^2H$/15N-labeled SRY/DNA–EDTA-Mn$^{2+}$ complex (0.3 mM). Sixty-four scans per FID were acquired for the 2-time-point measurement and 16 scans per FID for the 8-time-point measurement, resulting in the same total measurement time (~21 h). Identical measurements were carried out for the paramagnetic (Mn$^{2+}$) and diamagnetic (Ca$^{2+}$) states. The data were measured at a $^1H$-frequency of 500 MHz.](33) With a shorter repetition delay, $T_{rep}$, the recovery levels for the paramagnetic sample are always higher than those for the corresponding diamagnetic sample owing to the PRE on longitudinal relaxation rates ($T_1$). When this effect is taken into account, Eq. (7) is modified to
\[ I_{\text{para}}(0) = I_{\text{dia}}(0) \frac{1 - \exp\left(-R_{1,\text{dia}} + \Gamma_1 T_{\text{rep}}\right)}{1 - \exp\left(-R_{1,dia} T_{\text{rep}}\right)} \times \frac{R_{2,dia}}{R_{2,dia} + \Gamma_2} \exp\left(-\Gamma_2 \tau\right) \]

(8)

From the Solomon–Bloembergen equations, \( \Gamma_1 \) can be calculated from \( \Gamma_2 \) as follows:

\[ \Gamma_1 = \left[ \frac{2}{3} \frac{\omega_H^2 \tau^2}{3} + \frac{7}{6} \right]^{-1} \]

(9)

where \( \omega_H/2\pi \) is the \( ^1\text{H} \) frequency. Fig. 4 shows the theoretical relationship between the true \( \Gamma_2 \) and the apparent \( \Gamma_2 \) derived from the single-time-point approach \( (\Gamma_{2,\text{SP}}) \) using Eqs. (8) and (9). Depending on the PRE correlation time \( \tau_c \), the value of \( \Gamma_{2,\text{SP}} \) can be significantly smaller than the true \( \Gamma_2 \) value, especially for deuterated molecules. In the case of the PRE arising from Mn\( ^{2+} \) (where \( \tau_c \) is much smaller than that for a nitroxide spin label), the single time-point approach only yields accurate \( \Gamma_2 \) values when the repetition delay exceeds \( 4/R_{1,dia} \). The requirement of a long repetition delay makes the single-time-point approach less attractive, because multiple time-points can be acquired with a shorter delay and therefore a comparable overall experiment time. Another practical problem of the single time-point approach is that either an exponential window function or no window function at all must be employed for the \( ^1\text{H} \) dimension since Eq. (7) assumes a Lorentzian line-shape. In practice, this type of data processing is suboptimal for relatively large systems because Lorentzian shapes are broad and hence significantly decrease the number of analyzable peaks owing to partial overlaps. In addition, the single time-point approach requires the use of an appropriate scaling factor to account for slight differences in sample concentrations while multiple time-point methods do not. For a small protein, enhanced relaxation rates and decreased peak intensities are observed for virtually all residues in the presence of a paramagnetic probe, making it difficult to scale the two spectra reliably. For these reasons, it is our view that the single time-point approach should be restricted to qualitative use, especially for deuterated proteins.

3.5. Field-dependence of \(^1\text{H}\)-\( \Gamma_2 \)

In this section, we describe the field-dependence of \(^1\text{H}\)-\( \Gamma_2 \). Since \( \Gamma_2 \) for a macromolecule is dominated by the value of the spectral density function at zero frequency, \(^1\text{H}\)-\( \Gamma_2 \) rates measured at high magnetic field \((B_0 > 10 \text{T})\) should...
be dependent on $B_0$ if (a) the PRE correlation time $\tau_c$ is field-dependent, or (b) the contribution from Curie-spin relaxation (whose rate is proportional to $B_0^2$) is non-negligible. According to Gueron [34], $I_2$ due to the Curie-spin relaxation mechanism is given by

$$I_{2,\text{Curie-spin}} = \frac{1}{5} \left( \frac{\mu_0}{4\pi} \right)^2 \frac{\omega_H^2 g_b^4 h^4 \Delta^2 (S + 1)^2}{(3kT)^2} \times \left( 4\tau_c + \frac{3\tau_c}{1 + (\omega_H \tau_c)^2} - 4\tau_c - \frac{3\tau_c}{1 + (\omega_H \tau_c)^2} \right)$$

(10)

where $k$ is the Boltzman constant, and $T$ the temperature in Kelvin (Sometimes the last two negative terms in Eq. (10) are neglected, but this is only valid when $\tau_s \ll \tau_c$). In the case of the SRY/DNA–EDTA-Mn$^{2+}$ complex, the rotational correlation time $\tau_s$ is 8.5 ns from $^{15}$N relaxation data, and the PRE correlation time $\tau_c$, derived from the PRE $\Gamma_1$ and $\Gamma_2$ data, is 4.5 ns [20]. Thus, the electron relaxation time $\tau_e$ is calculated to be 9.6 ns [20]. For this system, Eqs. (3) and (10) predict that the contribution of the Curie-spin relaxation mechanism to the overall $\Gamma_2$ at 308 K is only 2%, even at a $^1$H-frequency of 800 MHz. The relative contribution of the Curie-spin relaxation depends on the size of the system. For a very large system with $\tau_s$ larger than 50 ns (corresponding to a molecular weight in excess of 100 kDa), the contribution could be larger than 20% at 800 MHz. In the case of a nitroxide spin label, the electron spin relaxation time $\tau_e$ ($>10^{-7}$ s) is much longer than $\tau_s$ [35,36] and, therefore, the PRE correlation time $\tau_c$, defined as $(\tau_s^{-1} + \tau_c^{-1})^{-1}$, is virtually identical to $\tau_e$, resulting in a field-independent $^1$H-$\Gamma_2$. For a macromolecular system with conjugated EDTA-Mn$^{2+}$, on the other hand, $\tau_s$ is comparable to $\tau_e$ [10,19,20] and consequently $^1$H-$\Gamma_2$ could be field-dependent because of the field-dependence of $\tau_e$.

To examine the field-dependence of $^1$H-$\Gamma_2$ arising from Mn$^{2+}$, we measured $^1$H-$\Gamma_2$ rates for the $^{13}$C/$^{15}$N-labeled SRY/DNA–EDTA-Mn$^{2+}$ complex at $^1$H-frequencies of 500, 600, and 800 MHz. Fig. 5 shows the correlations between the $\Gamma_2$ rates measured at the different fields. Linear regressions indicate that the $^1$H-$\Gamma_2$ rates at 600 and 800 MHz are higher than the corresponding rates at 500 MHz by factors of 1.02 and 1.08, respectively. (Note that these numbers are not precise because of experimental errors.) The field dependence of $^1$H-$\Gamma_2$ arising from Mn$^{2+}$ is very weak in this magnetic field range (11.7–18.8 T). This finding leads one to two conclusions. First, the contribution from Curie-spin relaxation is indeed negligible, which is consistent with the considerations described above. Second, the PRE correlation time $\tau_c$ is almost field-independent. Considering that the experimentally determined $\tau_c$ is smaller than the rotational correlation time $\tau_s$, this suggests a very weak field-dependence for the electron relaxation time $\tau_e$ of Mn$^{2+}$ at high magnetic field (>10 T) in contrast to the strong field dependence observed at low (<3 T) magnetic field [37].

Until recently, it was thought that the electron relaxation time $\tau_e$ for Mn$^{2+}$ is dominated by collisional modulation of the zero-field-splitting (ZFS) tensor, arising from distortion of a metal coordination system by collision with solvent molecules [37,38]. In this instance, $\tau_e$ should be proportional to $B_0^2$ at high magnetic fields that satisfy the condition $\omega_c \tau_e \gg 1$, where $\omega_c/2\pi$ is the electron Larmor frequency and $\tau_e$ the correlation time for collisional modulation of the ZFS tensor (usually on the order of $10^{-11}$ s). If this were the case, the ratio of the 800–500 MHz $^1$H-$\Gamma_2$ rates should be 1.52 for the SRY/DNA–EDTA-Mn$^{2+}$ complex whose rotational correlation time $\tau_s$ is 8.5 ns. Hence, this mechanism clearly does not explain our experimental observations.

Recently, Miller and Sharp pointed out that other contributions to the electron relaxation time $\tau_e$ need to be taken into account and that $\tau_e$ for a Mn$^{2+}$ system is actually given by [39]

$$\tau_e^{-1} = \tau_{\text{rot}}^{-1} + \tau_{\text{vib}}^{-1} + \tau_{\text{coll}}^{-1}$$

(11)
The first term, $\tau^{-1}_{s,\text{col}}$, is due to collisional modulation of the ZFS tensor, which was discussed above. The second term, $\tau^{-1}_{s,\text{rot}}$, is the reorientational modulation of the ZFS tensor, but its contribution is negligible for a macromolecule. The third term, $\tau^{-1}_{s,\text{ vib}}$, is for electron relaxation due to vibrational modulation of the ZFS tensor, which is essentially field-independent. The contribution of $\tau^{-1}_{s,\text{col}}$ to the overall $\tau^{-1}$ could be dominant at high-magnetic field since the first term $\tau^{-1}_{s,\text{col}}$ is inversely proportional to $B^2$. In fact, the magnitude of the ZFS tensor and the $\tau_s$ value reported for EDTA-Mn$^{2+}$ systems [40] predict a value $3 \times 10^6$ s$^{-1}$ for $\tau^{-1}_{s,\text{col}}$ at 11.7 T, which is significantly smaller than the experimentally measured value of $1.0 \times 10^5$ s$^{-1}$ for $\tau^{-1}$. Judging from our $^1\text{H}-\Gamma_2$ data, it is likely that the field-independent term $\tau^{-1}_{s,\text{ vib}}$ is dominant in overall electron relaxation at high magnetic fields between 11.7 and 18.1 T, whereas $\tau^{-1}_{s,\text{col}}$ is dominant at low magnetic fields.

3.6. Effect of diamagnetic contamination on $^1\text{H}-\Gamma_2$

In practice, no matter how carefully a paramagnetic sample may be prepared, contamination by trace amounts ($\sim 1\%$–$5\%$) of the corresponding diamagnetic species is almost impossible to avoid for the following reasons: (a) incomplete conjugation of the extrinsic paramagnetic group and insufficient purification of the conjugated species; (b) the presence of diamagnetic impurities in the paramagnetic stock solution (e.g. trace amounts of diamagnetic metals such as Zn$^{2+}$ and Ca$^{2+}$ in stock solutions of Mn$^{2+}$ for the EDTA-Mn$^{2+}$ system; the reduced species for a nitroxide spin label); (c) chemical instability of the conjugated states (discussed in a later section). Thus, it is important to ascertain the impact of diamagnetic contamination on the measured $^1\text{H}-\Gamma_2$ data.

Under conditions where the chemical shifts for the diamagnetic and paramagnetic states are identical and they do not exchange with each other, the signal intensity for the paramagnetic sample containing a trace amount of the diamagnetic species with population $p_d$ is given by

$$I(T) = (1 - p_d)I_{\text{para}}(T) + p_dI_{\text{dia}}(T) \quad (12)$$

Using Eqs. (1), (2), (5), (7), and (12), we calculated the theoretical relationship between the true value of $^1\text{H}-\Gamma_2$ and the apparent value that would be obtained from a two-time-point measurement for two values of $\Delta T$ and diamagnetic contaminations ranging from 0% to 5% (Fig. 6). The apparent value $\Gamma_2$ is always smaller than the true value. For the case with $R_{\text{dia}} = 50$ s$^{-1}$, $\Gamma_2 = 60$ s$^{-1}$, $p_d = 2\%$, the apparent value of $\Gamma_2$ from the two-time-point measurement with $\Delta T = 18$ ms is $52$ s$^{-1}$. For $p_d = 5\%$, the apparent value of $\Gamma_2$ is reduced to $44$ s$^{-1}$. Note that the percentage error in $\Gamma_2$ is much larger than $p_d$. This is due to the fact that the PRE significantly reduces the contribution of the first term in Eq. (12). The deviation from the true value of $\Gamma_2$ can be reduced by using a relatively small value of $\Delta T$, thereby reducing the relative contribution of the second term. For example, the apparent values of $\Gamma_2$ obtained with $\Delta T = 6$ ms are $55$ s$^{-1}$ for $p_d = 2\%$ and $48$ s$^{-1}$ for $p_d = 5\%$.

Fig. 7a shows correlations between experimental $^1\text{H}_\gamma-\Gamma_2$ data measured with $\Delta T = 4$ and 40 ms on $^{15}$N-HPt(E32C) conjugated with EDTA-Mn$^{2+}$ at Cys32. As expected from the above considerations, the measured $\Gamma_2$ values derived from the experiment with $\Delta T = 40$ ms are systematically smaller than those obtained with $\Delta T = 4$ ms, indicating the presence of a diamagnetic impurity. From this correlation, $p_d$ was estimated to be 3%. The same population for the diamagnetic impurity can also obtained from the intensities of residual peaks that should be completely broadened beyond detection, yet appear with low intensity because of the diamagnetic contamination (Fig. 7b).

In the case of intermolecular PRE measurements on a complex where dissociation and association processes are in fast exchange on the relaxation time scale, the observed $\Gamma_2$ is simply scaled down by $1 - p_d$ and the effect of a

Fig. 6. Theoretical effect of contamination by an equivalent diamagnetic species in a paramagnetic sample on $\Gamma_2$ accuracy. The relationship between the true values of $\Gamma_2$ and the apparent values derived from two time-point measurements ($I_{\text{app}}$) at different levels of diamagnetic contamination were computed using Eqs. (1), (2), (5), (7), and (12) for $\Delta T$ values of (a) 6 ms and (b) 18 ms. The curves shown are for contaminant population $p_d$ of 0%, 1%, 2%, 3%, and 5% as indicated in the panels.
3.7. Considerations of sample stability for $^1\text{H-}\Gamma_2$ measurements

Since a relatively small percentage of diamagnetic contamination can affect $^1\text{H-}\Gamma_2$, another concern is the stability of the paramagnetic sample itself. In the case of EDTA-conjugation to proteins, disulfide bond linkage to a Cys side-chain is commonly used [9,41–43]. As the reaction is reversible, the conversion rate cannot be 100% and there is always a small percentage of unconverted diamagnetic species. Although the desired product after the conjugation reaction can be purified by ion-exchange chromatography [28] or organic mercury columns [5], undesired cross-linked protein dimer, which is diamagnetic, is gradually formed via disulfide exchange. We have found that for a 6-month-old sample comprising a cysteaminy1-EDTA-Mn$^{2+}$ conjugate of $^{15}$N-labeled HPr(E32C), the dimer population can be as high as 30%, as confirmed by electrophoresis and mass spectrometry (data not shown). Therefore, a freshly prepared sample should always be used for the measurement of PREs arising from Cys-EDTA-Mn$^{2+}$. Alternatively, different chemistry can be used for conjugation of the paramagnetic group. For example, both maleimide [44] and iodide [5,45] functional groups selectively and irreversibly react with a free sulphydryl group under mild conditions, enabling the paramagnetic center to be linked to the protein via a stable C–S bond.

On the other hand, we found no evidence of this problem for EDTA-derivatized DNA, presumably because the EDTA group is conjugated through a stable linker without a disulfide bond [19,46]. The SRY/DNA complex containing dT-EDTA-Mn$^{2+}$ exhibited the same $^1\text{H}_\text{obs-}\Gamma_2$ values with experimental errors even 2 years after the first measurement (data not shown).

4. Concluding remarks

In this paper, we have described various practical aspects of $^1\text{H-}\Gamma_2$ measurements at high magnetic fields ($^1\text{H}$ frequency $\geq 500$ MHz) as applied to macromolecules (proteins, nucleic acids, and their complexes). We show that the two-time-point measurement approach provides a simple means to accurately measure $^1\text{H-}\Gamma_2$ without requiring any fitting procedures or complicated error estimations. Optimal settings required to minimize the experimental errors are also discussed. Increasing time-points while sacrificing S/N ratio for individual spectra to complete the measurement within a given timeframe does not result in any improvement in the precision or accuracy of the $\Gamma_2$ rates. The single-time-point approach, on the other hand, which has been extensively used in the literature, yields inaccurate $^1\text{H-}\Gamma_2$ rates unless the magnetization recovery levels for the diamagnetic and paramagnetic samples are identical. The $^1\text{H-}\Gamma_2$ rates arising from conjugated EDTA-Mn$^{2+}$ are found to be virtually field-independent for a 20 kDa system at high magnetic field ($B_0 > 11$ T). This is relevant when experiments are carried out in a research environment with multiple NMR spectrometers operating at different magnetic fields. Finally, PRE measurements involving conjugation of the paramagnetic center via a labile disulfide bond should be carried out immediately after sample preparation since trace amounts of the diamagnetic species can cause significant underestimation of $\Gamma_2$ rates.

The PRE arising from unpaired electrons with an isotropic g-tensor located on EDTA-Mn$^{2+}$ or a nitroxide free radical conjugated via a flexible linker to the macromolecule of interest probably represents the only practical tool...
in paramagnetic NMR to characterize macromolecules that do not possess an intrinsic metal binding site or paramagnetic center. Although other observables, such as pseudo-contact shifts and cross-correlation involving Curie-spin relaxation, arising from unpaired electrons with an anisotropic g-tensor, have been shown to be useful for the investigation of metal-binding proteins [247–51], similar applications to macromolecules with an extrinsic paramagnetic group tend to problematic owing to various practical considerations (e.g. the presence of enantiomers in the EDTA coordination system and linker flexibility; cf. Refs. [10] and [52]). In conclusion, PRE measurements afford a wealth of highly valuable information related to both structure and dynamics of biological macromolecules [5–28], and the practical considerations described in this paper are important for optimal experimental design and data interpretation in such investigations.

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References


