

# Determination of three-dimensional structures of proteins by simulated annealing with interproton distance restraints. Application to crambin, potato carboxypeptidase inhibitor and barley serine proteinase inhibitor 2

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An automated method, based on the principle of simulated annealing, is presented for determining the three-dimensional structures of proteins on the basis of short (<5 Å) interproton distance data derived from nuclear Overhauser enhancement (NOE) measurements. The method makes use of Newton's equations of motion to increase temporarily the temperature of the system in order to search for the global minimum region of a target function comprising purely geometric restraints. These consist of interproton distances supplemented by bond lengths, bond angles, planes and soft van der Waals repulsion terms. The latter replace the dihedral, van der Waals, electrostatic and hydrogen-bonding potentials of the empirical energy function used in molecular dynamics simulations. The method presented involves the implementation of a number of innovations over our previous restrained molecular dynamics approach [Clore, G.M., Brünger, A.T., Karplus, M. and Gronenborn, A.M. (1986) *J. Mol. Biol.*, **191**, 523–551]. These include the development of a new effective potential for the interproton distance restraints whose functional form is dependent on the magnitude of the difference between calculated and target values, and the design and implementation of robust and fully automatic protocol. The method is tested on three systems: the model system crambin (46 residues) using X-ray structure derived interproton distance restraints, and potato carboxypeptidase inhibitor (CPI; 39 residues) and barley serine proteinase inhibitor 2 (BSPI-2; 64 residues) using experimentally derived interproton distance restraints. Calculations were carried out starting from the extended strands which had atomic r.m.s. differences of 57, 38 and 33 Å with respect to the crystal structures of BSPI-2, crambin and CPI respectively. Unbiased sampling of the conformational space consistent with the restraints was achieved by varying the random number seed used to assign the initial velocities. This ensures that the different trajectories diverge during the early stages of the simulations and only converge later as more and more interproton distance restraints are satisfied. The average backbone atomic r.m.s. difference between the converged structures is  $2.2 \pm 0.3$  Å for crambin (nine structures),  $2.4 \pm 0.3$  Å for CPI (eight structures) and  $2.5 \pm 0.2$  Å for BSPI-2 (five structures). The backbone atomic r.m.s. difference between the mean structures derived by averaging the coordinates of the converged structures and the corresponding X-ray structures is 1.2 Å for crambin, 1.6 Å for CPI and 1.7 Å for BSPI-2.

*Key words:* three-dimensional structure/crambin/CPI/BSPI-2/simulated annealing/distance restraints

## Introduction

Determining the three-dimensional structures of proteins from interproton distance data derived from NMR measurements presents a highly complex, non-linear optimization problem as the data are limited in their number, accuracy and range (<5 Å) and there are numerous false local minima along the convergence pathway. Over the past few years a number of methods with large radii of convergence have been developed to tackle this problem. These include distance geometry methods based on the metric matrix (Crippen and Havel, 1978; Kuntz *et al.*, 1979; Havel *et al.*, 1983; Havel and Wüthrich, 1984, 1985; Havel, 1986; Sippl and Scheraga, 1986), restrained least-squares minimization in torsion angle space with either a variable target function (Braun and Go, 1985) or a sequence of ellipsoids of constantly decreasing volumes, each of which contains the minimum of the target function (Billeter *et al.*, 1987), and restrained molecular dynamics (Clore *et al.*, 1985, 1986a; Kaptein *et al.*, 1985; Brünger *et al.*, 1986; Nilsson *et al.*, 1986). The first three methods are based solely on the use of geometric restraints comprising interproton distances, bond lengths, bond angles, planes and soft van der Waals repulsion terms. In contrast, the restrained molecular dynamics method makes use of a full empirical energy function (comprising bonded and non-bonded interactions) supplemented by an effective potential term representing the experimental interproton distances. In terms of computational requirements, the first three methods are comparable and approximately five times faster than restrained molecular dynamics. Restrained molecular dynamics, on the other hand, has the advantage that the structures generated tend to be better in energetic terms than those obtained using the other methods, particularly with respect to the non-bonded interactions. It is for this reason that we have regularly employed restrained molecular dynamics either for the entire structure determination or to refine converged structures generated by the metric matrix distance geometry method (Clore *et al.*, 1986b, 1987a,b,c,d,e). In our experience, restrained molecular dynamics refinement results not only in large improvements in the non-bonded contacts (i.e. van der Waals energy) as compared with the starting structures generated by distance geometry calculations, but also improves significantly the agreement with the experimental NMR data.

In this paper we present an alternative approach for the structure generation phase. This approach is based on the principle of simulated annealing (Kirkpatrick *et al.*, 1983). As originally described, the simulated annealing method makes use of the Monte Carlo algorithm (Metropolis *et al.*, 1953) to increase the temperature of the system temporarily in order to search for the global minimum region of the target function. In our application, we make use of Newton's equations of motion to achieve the same effect. The method, however, differs from conventional restrained molecular dynamics insofar that it is based purely on

geometric restraints and the non-bonded terms of the target function are represented by a simple repulsion term (i.e. this replaces the dihedral, van der Waals, electrostatic and hydrogen-bonding potentials of the empirical energy function used in molecular dynamics). This has the advantage of significantly reducing the computational time requirements to a level comparable with the other methods mentioned above. In addition, two further innovations over our previous restrained molecular dynamics approach are implemented. The first involves the introduction of an effective nuclear Overhauser effect (NOE) potential whose functional form for a given interproton interaction is dependent on the magnitude of the difference between the calculated and target distance. This circumvents the need to classify the distances into short ( $|i-j| \leq 5$ ) and long ( $|i-j| > 5$ ) range, a procedure which is somewhat arbitrary, and increases the likelihood of correct folding. The second involves the design and implementation of a protocol which is fully automatic and considerably more robust than those employed in our previously restrained molecular dynamics study on crambin. The novel method is illustrated using three examples. The first is the model system crambin with the same distance set derived from the crystal structure that we used before in our restrained molecular dynamics study (Brünger *et al.*, 1986; Clore *et al.*, 1986a) and in the comparison of the restrained molecular dynamics and metric matrix distance geometry methods (Clore *et al.*, 1987f). The second and third examples are derived from our NMR work on potato carboxypeptidase inhibitor (CPI) and barley serine proteinase inhibitor 2 (BSPI-2) and make use of the same experimental interproton distance data that were employed to solve their structures by a combination of distance geometry and restrained molecular dynamics calculations (Clore *et al.*, 1987d,e). These three particular examples were chosen as the proteins exhibit quite different structural features as well as different sizes: crambin (46 residues) is composed principally of two  $\alpha$ -helices and a mini-antiparallel  $\beta$ -sheet (Hendrickson and Teeter, 1981), BSPI-2 is a predominantly  $\beta$ -sheet protein with a small  $\alpha$ -helix and a large reactive site loop (McPhalen *et al.*, 1985), and CPI has little or no regular secondary structure (Rees and Lipscomb, 1982).

## Methods

All calculations were carried out on a CONVEX-C1XP computer using a modified version of the program XPLOR (Brünger *et al.*, 1987a,b) which is derived from the program CHARMM (Brooks *et al.*, 1983) and has been especially adapted for restrained molecular dynamics (e.g. Clore *et al.*, 1985, 1986a; Brünger *et al.*, 1986). Integration of the classical equations of motion was performed using a Verlet (1967) integration algorithm with initial velocities assigned to a Maxwellian distribution at an appropriate temperature. The time step of the integrator was 0.001 ps and the non-bonded contact list was updated every 0.008 ps. Displaying of trajectories was carried out using a modified version of the function network of FRODO (Jones, 1978) interfaced with XPLOR.

## Results and discussion

### The target function

The total target function  $F_{\text{tot}}$  for which the global minimum region is searched is made up of the following terms:

$$F_{\text{tot}} = F_{\text{covalent}} + F_{\text{repel}} + F_{\text{NOE}} \quad (1)$$

$F_{\text{tot}}$  in effect represents the potential energy of the system whose

units in the present calculations are kcal/mol. These units are purely arbitrary. Thus, the simulated annealing procedure employed in this case involves the simultaneous integration of Newton's equations of motion:

$$\frac{\partial^2 \mathbf{X}_i}{\partial t^2} = - \frac{1}{m_i} \frac{\partial}{\partial \mathbf{X}_i} F_{\text{tot}}(\mathbf{X}_1, \mathbf{X}_2, \dots, \mathbf{X}_n) \quad (2)$$

for all  $n$  atoms in the system whose temperature is given by

$$(\text{Temp})_i = \frac{2}{k_B(3n-6)} \left( \sum_{i=1}^n m_i v_i^2 / 2 \right) \quad (3)$$

$F_{\text{covalent}}$  is the target function for maintaining correct bond lengths, angles and planes, and is given by

$$F_{\text{covalent}} = \sum_{\text{bonds}} k_b(r-r_0)^2 + \sum_{\text{angles}} k_\theta(\theta-\theta_0)^2 + \sum_{\text{impropers}} k_\omega(\omega-\omega_0)^2 \quad (4)$$

The values chosen for the force constants for the bond ( $k_b$ ), angle ( $k_\theta$ ) and improper torsions ( $k_\omega$ ) are set to uniform high values to ensure near perfect stereochemistry throughout the calculations, namely 600 kcal/mol/Å<sup>2</sup>, 500 kcal/mol/rad<sup>2</sup> and 500 kcal/mol/rad<sup>2</sup> respectively. (Note that the improper torsion terms serve to maintain planarity and chirality.)

$F_{\text{repel}}$  is the target function used to prevent unduly close non-bonded contacts and is given by

$$F_{\text{repel}} = \begin{cases} 0 & \text{if } r \geq s \cdot r_{\text{min}} \\ k_r(s^2 \cdot r_{\text{min}}^2 - r^2)^2 & \text{if } r < s \cdot r_{\text{min}} \end{cases} \quad (5)$$

The values of  $r_{\text{min}}$  are the standard values of the van der Waals radii as represented by the Lennard-Jones potential used in the CHARMM empirical energy function (Brooks *et al.*, 1983);  $s$  is a van der Waals radius scale factor, and  $k_r$  the van der Waals repulsion force constant. It should also be noted that the large reduction in the computational time required to evaluate  $F_{\text{repel}}$  compared with the usual full non-bonded interaction potential represented in the empirical energy function is due not only to the smaller number of terms that have to be calculated but also to a reduction in the number of pairs that have to be included in the non-bonded contact list. Thus, in the case of  $F_{\text{repel}}$  the non-bonded contact list comprises only all pairs up to 4.5 Å, compared with pairs up to 8 Å in the case of the full empirical non-bonded energy function.

$F_{\text{NOE}}$  is the NOE target function and is a complex term made up of three terms  $F_{\text{long}}$ ,  $F_{\text{short}}$  and  $F_{\text{final}}$ , whose functional form depends on the difference between the calculated ( $r_{ij}$ ) and target ( $r_{ij}^0$ ) value of a particular interproton distance, as well as on the value of the variable force constant for the  $F_{\text{short}}$  term (see below). Our previous restrained molecular dynamics calculations have used biharmonic (Clore *et al.*, 1985) and square well (Clore *et al.*, 1986b) potentials. Such forms, however, give rise to severe problems in simulations that start from initial structures containing large violations between calculated and target distance values. It was for this reason, for example, that in our restrained dynamics model calculations on crambin starting from an extended strand, distances between residues separated by more than five residues in the sequence were initially excluded from the calculation and only introduced at a later stage once partial folding of the helices had occurred.

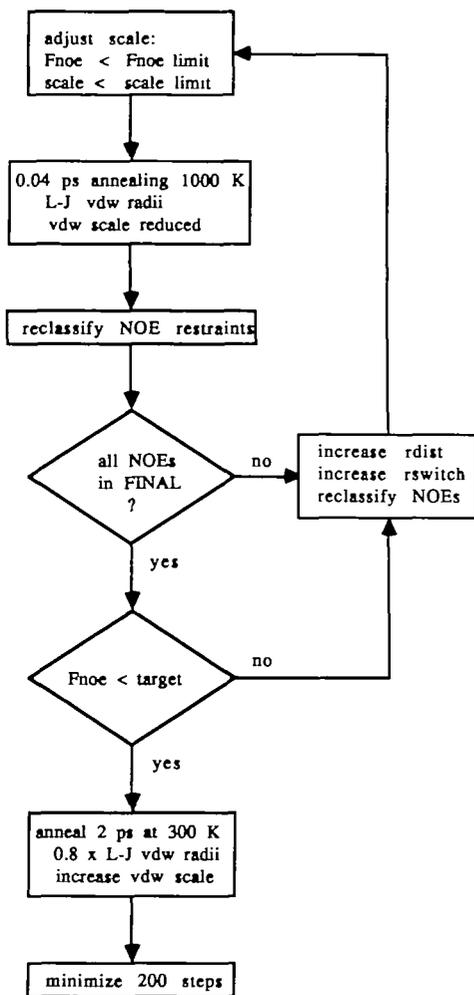


Fig. 1. Simplified flowchart of the simulated annealing protocol (L–J signifies Lennard–Jones).

### Calculational strategy

A simplified flowchart of the calculational strategy is shown in Figure 1. Its design is based on three guidelines: (i) that secondary structure elements should be formed prior to tertiary structure folding; (ii) that converged NOE restraints and/or local structure elements once formed should be retained; and (iii) that the incorporation of NOE restraints into the NOE target function  $F_{\text{NOE}}$  should be completely automatic [i.e. that no special treatment of the NOE data, as was done for our previous restrained molecular dynamics calculations (Clore *et al.*, 1986a), should be necessary before the start of the simulation]. To achieve these aims, the NOE violations are analysed and grouped into different classes, depending on their size (see description below), at the end of each cycle of simulated annealing, and a special potential form is used that places greater weight on smaller violations. A further requirement is that the value of the target function  $F_{\text{NOE}}$  should not exceed certain limits for technical reasons. This necessitates the automatic adjustment of the NOE force constants, as appropriate, during the course of the simulation.

The calculations have to start from unfolded structures (e.g. an extended strand) rather than from entirely random structures which may already be folded. The reason for this is that once the polypeptide chain has folded incorrectly it can no longer converge to the correct global minimum region. The random

number seed, however, used for the assignment of the initial velocities is sufficient to ensure good sampling of the available conformational space consistent with the interproton distance data (see following section).

The NOE restraints are initially classified into two classes, *long* and *short*, depending on the difference ( $\text{viol}_{ij}^u$ ) between the calculated ( $r_{ij}$ ) and upper limit of the target ( $r_{ij}^u$ ) distances. Class *long* contains NOE restraints which are violated by more than  $\text{rdist}_{\text{LS}}$ , class *short* contains all the others. In class *long* the target function is switched off (i.e.  $F_{\text{long}} = 0$ ). In class *short* the target function has the following functional form:

$$F_{\text{short}} = \begin{cases} k_s(c \cdot \text{viol}_{ij}^u + \frac{b}{\text{viol}_{ij}^u} + a) & \text{if } \text{viol}_{ij} > \text{rswitch} \\ k_s(\text{viol}_{ij}^u)^4 & \text{if } r_{ij} > r_{ij}^u \text{ and } \text{viol}_{ij}^u \leq \text{rswitch} \\ 0 & \text{if } r_{ij}^l \leq r_{ij} \leq r_{ij}^u \\ k_s(\text{viol}_{ij}^l)^4 & \text{if } r_{ij} < r_{ij}^l \end{cases} \quad (6)$$

The values of  $a$  and  $b$  are chosen such that  $F_{\text{short}}$  is continuous and differentiable at  $\text{rswitch}$ . They are given by

$$\begin{aligned} a &= 5\text{rswitch}^4 - 2c \cdot \text{rswitch} \\ b &= -4\text{rswitch}^5 + c \cdot \text{rswitch}^2 \end{aligned} \quad (7)$$

$c$ , the slope of the asymptote, is set to 0 in the present calculations. The initial values chosen for  $\text{rswitch}$ ,  $\text{rdist}_{\text{LS}}$  and the force constant  $k_s$  are 3 Å, 10 Å and 0.05 kcal/mol/Å<sup>2</sup> respectively.

A diagram of the functional form of  $F_{\text{short}}$  is shown in Figure 2. This potential form is designed to ensure that secondary structure elements defined by interproton distances between residues close together in the sequence are formed prior to the incorporation of NOEs between residues far apart in the sequence. The gradient of  $F_{\text{short}}$  is largest at  $\text{rswitch} + r_{ij}^u$  so that NOEs which are violated by about the value of  $\text{rswitch}$  experience the largest force. At the beginning of the simulation  $\text{rswitch}$  is set to a low value ( $\sim 3$  Å); by progressively increasing its value, the maximum of the driving force is shifted to larger violations. Thus once the formation of local secondary structures such as  $\alpha$ -helices has occurred, turns can be formed and tertiary structure folding can gradually take place. For the same reason, NOEs that are violated by more than  $\text{rdist}_{\text{SL}}$  are placed in a class *long* where they experience no force from the NOE restraints at all.

At the beginning of the calculations the hard sphere radii of the atoms are chosen as in the Lennard–Jones potential (i.e.  $s$  in equation 5 is set to 1.0). The calculations are initiated with 20 steps of Powell (1977) minimization to remove some bad non-bonded contacts. This is followed by Phase 1 of the simulated annealing protocol. The initial velocities at  $t = 0$  ps are chosen from a Maxwellian distribution at 1000K. This temperature is chosen to ensure that local minima along the convergence pathway towards the global minimum region of the target function  $F_{\text{tot}}$  can be overcome. Each cycle of annealing comprises 40 steps with a time step of 1 fs in which the non-bonded contact list is updated every eight steps and the velocities are rescaled to 1000K every 20 steps. After every cycle of annealing the force constant  $k_s$  for  $F_{\text{short}}$  is increased up to a maximum value of 15.8 kcal/mol/Å<sup>2</sup> by multiplying its value by 10<sup>0.1</sup>. The value of  $F_{\text{NOE}}$  is then evaluated with the new value of  $k_s$ , and if  $F_{\text{NOE}}$

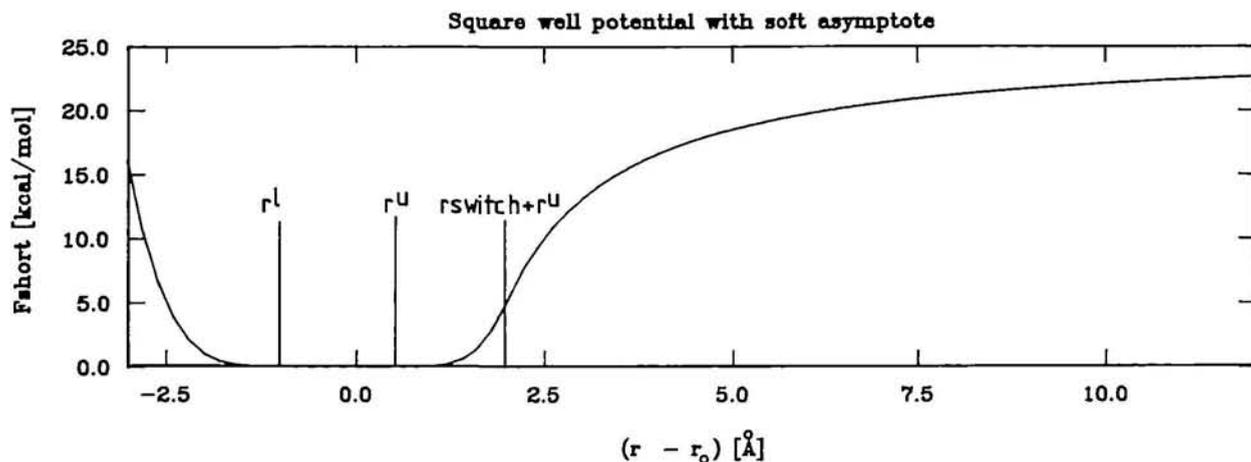


Fig. 2. Potential form of  $F_{\text{short}}$  (equation 6) for  $r_0 = 3.0 \text{ \AA}$ ,  $k_s = 1.0 \text{ kcal/mol/\AA}^2$ ,  $r^l = 2.0 \text{ \AA}$ ,  $r^u = 3.5 \text{ \AA}$ ,  $r_{\text{switch}} = 1.5 \text{ \AA}$  and  $c = 0$ . The positions of  $r^l$ ,  $r^u$  and  $r_{\text{switch}} + r^u$  are indicated.

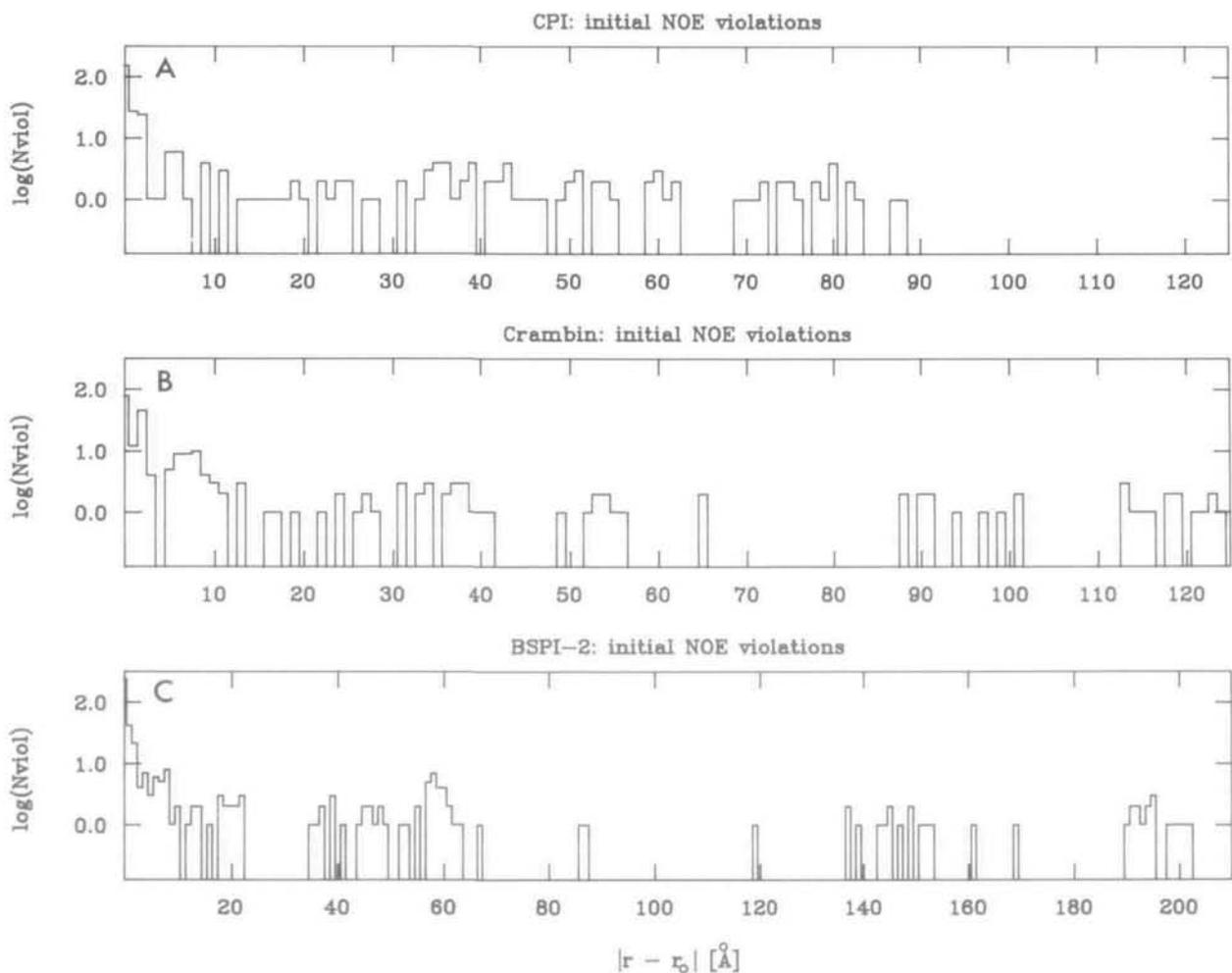


Fig. 3. Histogram showing the distribution of the number of NOE violations  $N_{\text{viol}}(r_{ij} > r_{ij}^u)$  as a function of the value of the violation  $(r_{ij} - r_{ij}^u)$  in the initial extended strand structures of CPI, crambin and BSPI-2. The  $\Delta$  interval for counting  $N_{\text{viol}}$  is  $1 \text{ \AA}$ . Note that the vertical scale is logarithmic.

$> 2500 \text{ kcal/mol}$   $k_s$  is divided by  $10^{0.1}$  until  $F_{\text{NOE}} < 2500 \text{ kcal/mol}$ . Once  $k_s$  has reached its maximum value of  $15.8 \text{ kcal/mol/\AA}^2$ , the NOE restraints are further reclassified between class *short* and class *final* if  $\text{viol}_{ij}^u$  is less than  $r_{\text{dist}_{\text{FS}}}$ . The value of  $r_{\text{dist}_{\text{FS}}}$  chosen is  $1.0 \text{ \AA}$ , and  $F_{\text{final}}$  is a square-well function with a force constant  $k_f$  of  $60 \text{ kcal/mol/\AA}^2$  which is never changed

$$F_{\text{final}} = \begin{cases} k_f (\text{viol}^u)^4 & \text{if } r_{ij} > r_{ij}^u \\ 0 & \text{if } r_{ij}^l \leq r_{ij} \leq r_{ij}^u \\ k_f (\text{viol}^l)^4 & \text{if } r_{ij} < r_{ij}^l \end{cases} \quad (8)$$

Thus class *final* contains all the NOE restraints which have converged. In addition, the restraints in the *long* and *short* classes

Table I. Atomic r.m.s. differences<sup>a</sup>

	Atomic r.m.s. difference (Å)					
	Crambin		CPI (residues 2–39) <sup>b</sup>		BSPI-2 (residues 22–83) <sup>c</sup>	
	Backbone atoms	All atoms	Backbone atoms	All atoms	Backbone atoms	All atoms
Ini versus SA	38.4	38.3	33.2	33.8	58.0	58.1
<SA> versus <SA>	2.2 ± 0.3	2.7 ± 0.4	2.4 ± 0.3	3.4 ± 0.5	2.5 ± 0.2	3.6 ± 0.3
<SA> versus $\overline{SA}$	1.5 ± 0.3	1.8 ± 0.4	1.6 ± 0.3	2.3 ± 0.4	1.6 ± 0.2	2.3 ± 0.2
SA versus $(\overline{SA})_r$	0.5	0.7	0.6	0.8	0.7	0.9
<SA> versus $(\overline{SA})_r$	1.6 ± 0.3	1.9 ± 0.4	1.7 ± 0.3	2.5 ± 0.5	1.7 ± 0.2	2.4 ± 0.2
<DG> versus <DG>	1.8 ± 0.2	2.7 ± 0.3	1.7 ± 0.2	2.5 ± 0.5	1.6 ± 0.1	2.7 ± 0.1
<DG> versus $\overline{DG}$	1.2 ± 0.1	1.8 ± 0.1	1.2 ± 0.1	1.7 ± 0.2	1.1 ± 0.1	1.8 ± 0.1
<RD> versus <RD>	2.1 ± 0.2	2.7 ± 0.1				
<RD> versus $\overline{RD}$	1.4 ± 0.2	1.7 ± 0.1				
<RDDG> versus <RDDG>			2.1 ± 0.4	2.8 ± 0.4	2.1 ± 0.3	3.1 ± 0.3
<RDDG> versus $\overline{RDDG}$			1.4 ± 0.3	1.9 ± 0.3	1.4 ± 0.2	2.1 ± 0.1
$\overline{SA}$ versus $\overline{DG}$	1.3	1.8	1.3	1.7	1.4	2.0
$\overline{SA}$ versus $\overline{RD}/\overline{RDDG}$	1.3	1.7	1.8	2.4	1.5	2.0
$\overline{DG}$ versus $\overline{RD}/\overline{RDDG}$	1.2	1.7	1.5	1.8	2.0	2.5
<SA> versus X-ray	1.9 ± 0.3	2.5 ± 0.5	2.2 ± 0.3	3.3 ± 0.4	2.3 ± 0.2	3.3 ± 0.3
$\overline{SA}$ versus X-ray	1.2	1.7	1.6	2.5	1.7	2.4
$(\overline{SA})_r$ versus X-ray	1.2	1.8	1.8	2.7	1.7	2.5
$\overline{DG}$ versus X-ray	1.3	2.1	1.4	2.2	1.9	2.7
$\overline{RD}/\overline{RDDG}$ versus X-ray	1.1	1.4	1.6	2.3	1.4	2.3

<sup>a</sup>The notation of the structures is as follows: Ini, the extended  $\beta$ -strand starting structure for the simulated annealing calculations; <SA>, the converged structures produced by simulated annealing starting out from the extended  $\beta$ -strand structure Ini; <DG>, converged structures obtained by metric matrix distance geometry calculations using the program DISGEO (Havel, 1986); <RD> and <RDDG>, converged restrained molecular dynamics structures obtained starting from an extended strand and converged <DG> structures respectively;  $\overline{SA}$ ,  $\overline{DG}$ ,  $\overline{RD}$  and  $\overline{RDDG}$ , the mean structures obtained by averaging the coordinates of the <SA>, <DG>, <RD> and <RDDG> structures respectively;  $(\overline{SA})_r$  is the structure derived by restrained Powell minimization of the mean  $\overline{SA}$  structure. There are nine SA structures for crambin, eight for CPI and five for BSPI-2. The X-ray structures of crambin, CPI and BSPI-2 are from Hendrickson and Teeter (1981), Rees and Lipscomb (1982) and McPhalen and James (1987). The <RD> and <DG> structures of crambin are from Clore *et al.* (1986a) and (1987f) respectively; there are five <RD> structures and seven <DG> ones. The <DG> and <RDDG> structures of CPI and BSPI-2 are from Clore *et al.* (1987d) and (1987e) respectively; there are 11 structures of each type. (Note that in the case of CPI and BSPI-2 all the restrained molecular dynamics structures are obtained starting from converged <DG> structures, while in the case of crambin, they are all obtained starting out from extended type structures.)

<sup>b</sup>Best fitting in the case of CPI was performed with respect to residues 2–39 as no NOEs involving residue 1 were observed (Clore *et al.*, 1987d) In comparisons with the X-ray structure of CPI, best fitting is carried out with respect to residues 2–38, as residue 39 is cleaved from the protein in the CPI–carboxypeptidase complex from which the X-ray structure of CPI is derived (Rees and Lipscomb, 1982).

<sup>c</sup>In the case of BSPI-2 the best-fits are carried out with respect to residues 22–83 as no NOEs could be detected involving residues 20–21. Note that the NMR on BSPI-2 was carried out on the 64-residue proteolytic fragment comprising residues 20–83 as the first 19 residues are disordered both in solution (Kjaer *et al.*, 1987; Kjaer and Poulsen, 1987) and in the crystal structures (McPhalen *et al.*, 1985; McPhalen and James, 1987).

are counted and the smallest violation in class *long* is calculated. Three cases are distinguished: (i) if both the *long* and *short* classes are empty and  $F_{\text{NOE}}$  has a value below its target value (in this case 120 kcal/mol), global as well as local convergence has occurred, the Phase 1 calculation is stopped and the simulation proceeds directly to Phase 2 of the annealing protocol; (ii) if only the *short* class is empty and the value of  $F_{\text{NOE}}$  lies below its target value, ‘local convergence’ has been achieved, and the value of  $rdist_{\text{LS}}$  for the reclassification between classes *long* and *short* is set to just above (0.02 Å) the smallest violations in class *long* so that one or only a few additional violations go into class *short*; and (iii) if neither case (i) nor case (ii) applies then  $rdist_{\text{LS}}$  is increased by 0.02 Å. Additionally, in cases (ii) and (iii) the value of  $rswitch$  is increased by 0.01 Å and the NOE restraints are reclassified between classes *long* and *short*.

The rationale behind the grouping of all ‘converged NOE restraints’ in class *final* is to ensure that once secondary structure elements have formed they are preserved and not disrupted at a later stage during the course of the simulation. This is required since there is no force other than the NOE restraints to stabilize such secondary structure elements, and the scale of the *short*

potential has to be reduced drastically at times as longer-range NOEs are incorporated into  $F_{\text{short}}$ . For this reason the force constant on the *final* potential is never reduced. To ensure that the reclassification only takes place once NOEs have really converged and to allow some rearrangement of the local structure, NOEs are only reclassified between the *final* and *short* classes when the force constant for  $F_{\text{short}}$  is at its maximum value.

After every 10 cycles of annealing, the velocities are partially (~25%) rerandomized by adding the *x*, *y* and *z* components of the velocities assigned at 300K to the existing velocities and dividing the resulting new velocities by  $\sqrt{1.3}$  to restore the velocities back to a temperature of 1000K. This is done to slow down large-scale rigid body motions and to introduce a further random element into the protocol, in addition to that arising from the variation in the random number seed used to assign the initial velocities at the beginning of Phase 1. The random element arises insofar that a partial rerandomization of the velocities may change the direction of motion of the atoms in a non-deterministic manner.

The maximum number of cycles for Phase 1 was 250 for CPI and crambin, and 350 for BSPI-2 (the larger the protein, the more

**Table II.** NOE deviations and violations, deviations from ideality, van der Waals energies and radii of gyration<sup>a</sup>

Structure	NOE <sub>r.m.s.</sub> <sup>b</sup> (Å)	NOE <sub>viol</sub> <sup>b</sup>	Deviations from ideality			Van der Waals energy <sup>c</sup> (kcal/mol)	Radii of gyration (Å)
			Bonds (Å)	Angles (deg)	Impropers (deg)		
<b>Crambin</b>							
No. of terms	249		642	1177	143		
Ini	35.3	173	0.017	2.58	0.23	289	42.54
<SA>	0.12 ± 0.11	0.6 ± 0.5	0.010 ± 0.004	2.78 ± 0.40	0.20 ± 0.04	-113 ± 18	9.99 ± 0.15
$\overline{SA}$	0.03	0	0.436	23.53	5.17	>10 <sup>6</sup>	9.82
( $\overline{SA}$ ) <sub>r</sub>	0.09	1	0.007	4.23	0.15	-76	10.04
<DG>	0.14 ± 0.04	1.9 ± 0.2	0.017 ± 0.001	3.79 ± 0.29	0.15 ± 0.05	230 ± 336	9.92 ± 0.08
<RD>	0.08 ± 0.01	0.6 ± 1.3	0.014 ± 0.002	3.94 ± 0.53	0.75 ± 0.12	-157 ± 10	9.38 ± 0.17
X-ray	0.02	0	0.020	2.87	1.48	-213	9.64
<b>CPI</b>							
No. of terms	318		565	1008	209		
Ini	27.7	147	0.074	4.33	0.34	468	38.79
<SA>	0.10 ± 0.01	0.1 ± 0.4	0.010 ± 0.003	3.48 ± 0.53	0.31 ± 0.07	-90 ± 27	9.93 ± 0.14
$\overline{SA}$	0.07	3	0.456	21.10	1.72	>10 <sup>6</sup>	8.82
( $\overline{SA}$ ) <sub>r</sub>	0.08	0	0.010	5.67	0.23	4	9.27
<DG>	0.14 ± 0.05	6.7 ± 4.5	0.021 ± 0.002	4.22 ± 0.27	2.71 ± 0.95	368 ± 1257 <sup>d</sup>	10.10 ± 0.10
<RDDG>	0.05 ± 0.01	0.09 ± 0.3	0.019 ± 0.003	4.26 ± 0.32	0.51 ± 0.04	-100 ± 28	9.08 ± 0.19
X-ray	0.41	24	0.24	5.00	3.34	841	9.29
<b>BSPI-2</b>							
No. of terms	403		1069	1961	265		
Ini	43.7	148	0.062	3.87	0.35	812	63.72
<SA>	0.10 ± 0.02	1.0 ± 1.7	0.007 ± 0.002	2.06 ± 0.38	0.37 ± 0.04	-180 ± 10	11.80 ± 0.21
$\overline{SA}$	0.10	2	0.48	22.80	1.13	>10 <sup>6</sup>	11.56
( $\overline{SA}$ ) <sub>r</sub>	0.08	0	0.008	4.35	0.20	-41	11.82
<DG>	0.17 ± 0.02	13.2 ± 3.4	0.020 ± 0.003	4.30 ± 0.28	3.07 ± 0.62	776 ± 669	11.57 ± 0.13
<RDDG>	0.06 ± 0.006	0.5 ± 0.7	0.021 ± 0.002	4.18 ± 0.21	0.73 ± 0.06	-145 ± 26	10.96 ± 0.14
X-ray	0.32	22	0.015	3.33	1.73	-224	11.27

<sup>a</sup>The notation of the structures is the same as that in Table I.

<sup>b</sup>NOE<sub>r.m.s.</sub> is the r.m.s. difference (r.m.s.d.) between the calculated ( $r_{ij}$ ) and target restraints, calculated with respect to the upper ( $r_{ij}^u$ ) and lower limits ( $r_{ij}^l$ ) such that

$$\text{r.m.s.d.} = \begin{cases} [(r_{ij} - r_{ij}^u)^2/n]^{1/2} & \text{if } r_{ij} > r_{ij}^u \\ 0 & \text{if } r_{ij}^l \leq r_{ij} \leq r_{ij}^u \\ [(r_{ij} - r_{ij}^l)^2/n]^{1/2} & \text{if } r_{ij} < r_{ij}^l \end{cases}$$

NOE<sub>viol</sub> is the number of violations for which  $r_{ij} > (r_{ij}^u + 0.5 \text{ \AA})$ . The interproton distance restraints for crambin, CPI and BSPI-2 are taken from Clore *et al.* (1986a), (1987d) and (1987e) respectively. In the case of crambin and CPI, the restraints include nine additional restraints for the three disulphide bridges present in these two proteins. Distances involving methyl and methylene protons are calculated using centre averaging with the same corrections to the upper limits of the target distances as that used in the essentially equivalent pseudo-atom representation (Wüthrich *et al.*, 1983).

<sup>c</sup>The van der Waals energy is calculated using the Lennard–Jones potential and parameters in the CHARMM empirical energy function (Brooks *et al.*, 1983). Note that this energy term is *not* included in the target function (cf. equation 1) whose global minimum is searched by simulated annealing. The only non-bonded contact term present in the target function is a hard-sphere repulsion term (cf. equation 5).

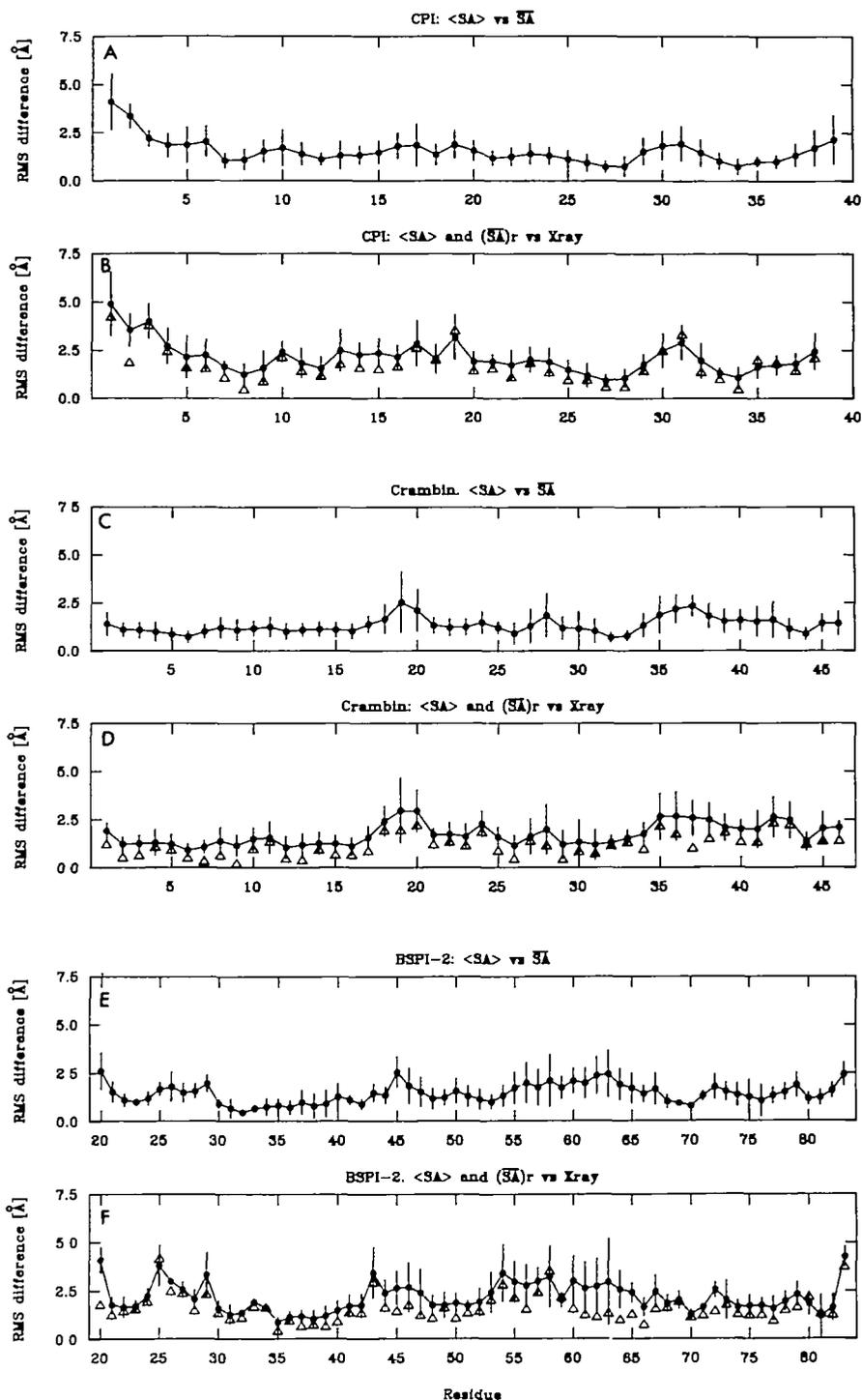
<sup>d</sup>The van der Waals energy for the <DG> structures of CPI range from -67 to 4248 kcal/mol.

cycles required). If at this stage there are still violations in class *long*, failure of convergence is presumed and the calculation comes to a complete halt. If, on the other hand, there are no violations in class *long*, the NOE restraints are once again reclassified between classes *short* and *final* at 10 Å in order to place all the NOEs into the *final* class. This is followed by Phase 2 of the annealing protocol which comprises 20 cycles of 100 steps of annealing at 300K. The velocities are rescaled to 300K after every cycle and the force constant  $k_r$  for the repulsion target function  $F_{\text{repl}}$  (cf. equation 5) is increased in steps of 0.2 from an initial value of 0.4 kcal/mol/Å<sup>2</sup> to a final value of 4 kcal/mol/Å<sup>2</sup>. The values of the hard sphere atom radii are set to 0.8 times their Lennard–Jones values (i.e.  $s = 0.8$  in equation 5). The resulting values are approximately the same as those used in the various distance geometry programs. The value of 4 kcal/

mol/Å<sup>2</sup> for the force constant  $k_r$  was found to be sufficient to ensure that no close non-bonded contacts occur. Finally, Phase 2 is followed by 200 steps of restrained Powell minimization to complete the simulation.

#### Calculations on crambin, CPI and BSPI-2

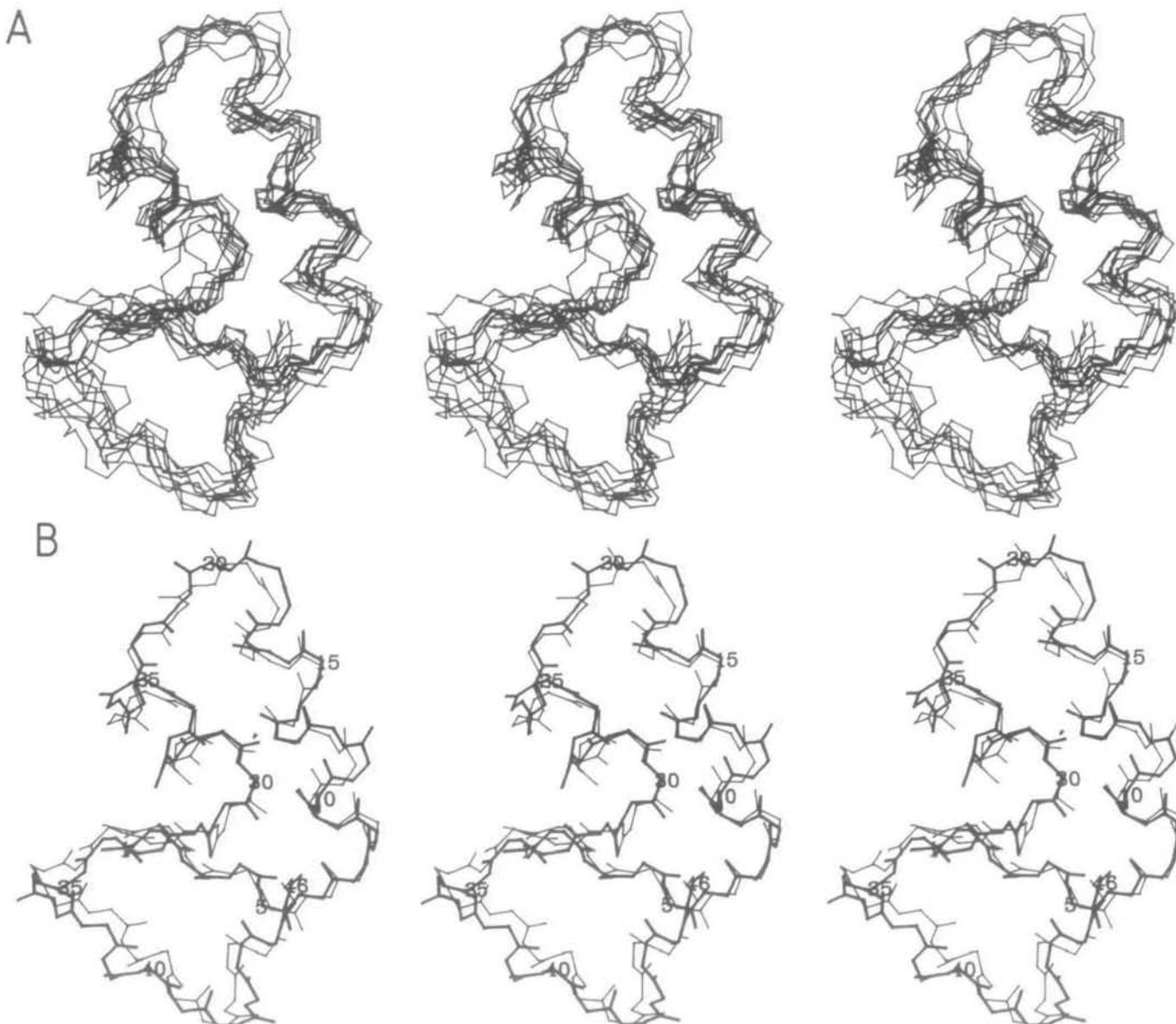
The calculations on crambin, CPI and BSPI-2 (the 64-residue proteolytic fragment comprising residues 20–83) were carried out starting from an extended β-strand (r.m.s. atomic difference of ~38 Å, ~33 Å and ~58 Å from the respective crystal structures) using the same NOE distance data set that was employed in our previous studies (Clore *et al.*, 1986a, 1987d,e). In the case of crambin the NOE data set consisted of 240 interproton distances derived from the crystal structure (Hendrickson and Teeter, 1981), while for CPI and BSPI-2 they comprised



**Fig. 4.** Atomic r.m.s. distribution of the backbone (C, C $\alpha$ , N, O) atoms of the <SA> structures about the mean structure  $\overline{SA}$  (A, C and E), and atomic r.m.s. difference between the <SA> ( $\bullet$ ) and (SA)r ( $\Delta$ ) structures on the one hand and the corresponding X-ray structures on the other (B, D and F) for CPI (A and B), crambin (C and D) and BSPI-2 (E and F). The filled-in circles ( $\bullet$ ) represent the average r.m.s. difference between the <SA> structures and either the mean  $\overline{SA}$  structure (A, C or E) or the X-ray structure (B, D and F), and the bars represent the standard deviations in these values. In the case of CPI, the <SA> structures are best fitted to residues 2–39 of the mean  $\overline{SA}$  structure (A) and to residues 2–38 of the X-ray structure (B); in the case of BSPI-2 all the best fits are carried out with respect to residues 22–83.

309 and 403 interproton distances, respectively, derived from NOE measurements. The lower limit ( $r_{ij}^l$ ) for all the restraints was 1.8 Å, while the upper limits ( $r_{ij}^u$ ) were set to 2.7, 3.3 and 5 Å, corresponding to strong, medium and weak NOEs. Figure 3 shows the distribution of NOE violations in the initial structures revealing violations up to 88, 125 and 203 Å for CPI, crambin

and BSPI-2 respectively. Note that crambin and BSPI-2 exhibit distinctive gaps in the distribution of the initial violations, while CPI shows a continuum of violations. As a result, class *short* is empty at several stages during the calculations in the case of crambin and BSPI-2, indicating that local convergence has occurred. For CPI, on the other hand, long-range NOE restraints

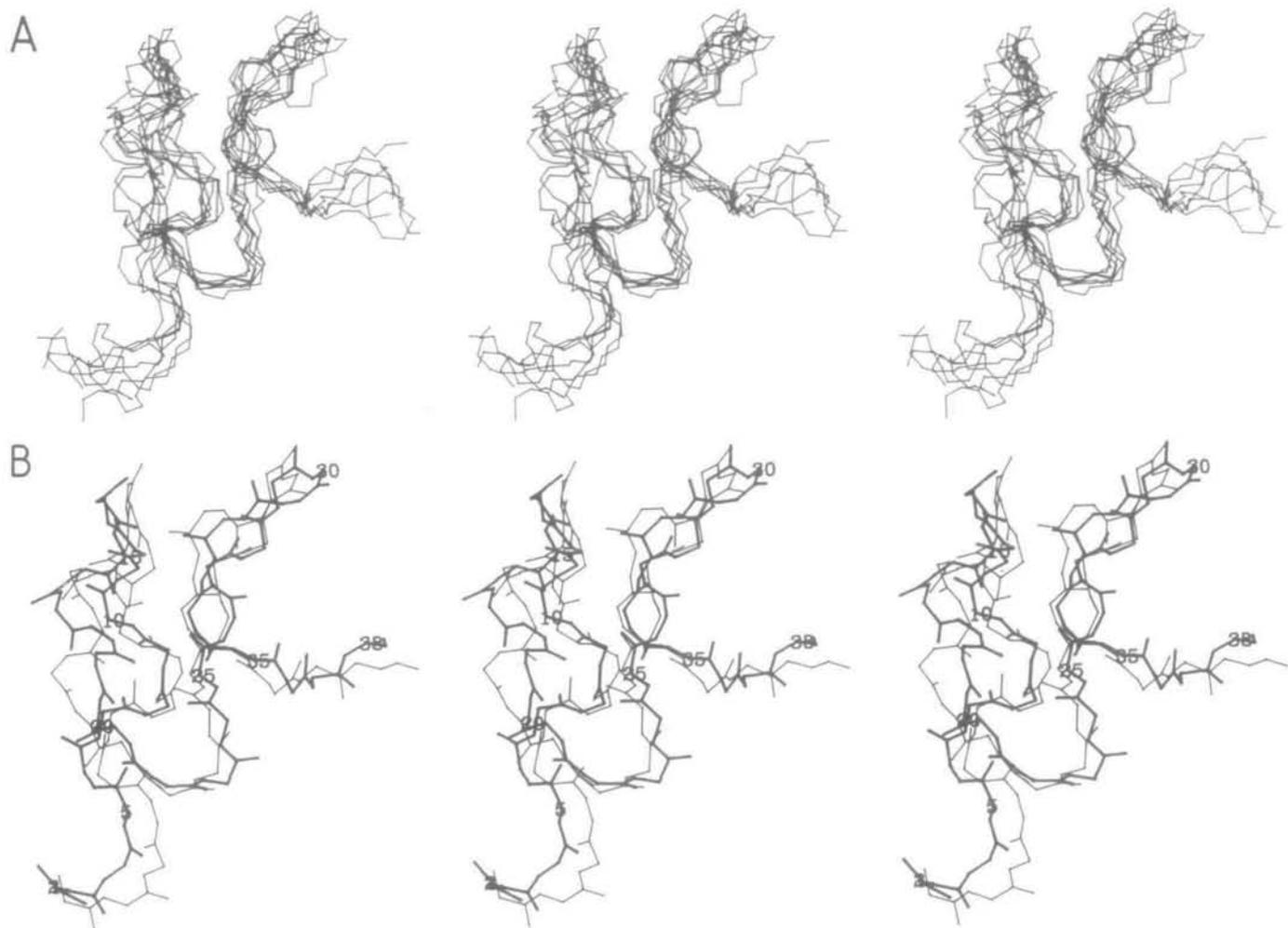


**Fig. 5.** (A) Best-fit superposition of the backbone (C, C $\alpha$ , N) atoms of the nine converged SA structures of crambin; (B) best-fit superposition of the backbone (C, C $\alpha$ , N, O) atoms of the (SA)r structure (thick lines) with the X-ray structure of crambin (thin lines). The three-picture stereo system used in this figure enables readers with both natural and cross-over stereo vision to view the images. For normal vision, select the left and centre images; for cross-over vision, use the centre and right images.

are taken into class *short* during almost the entire course of the calculations. In the case of distances involving methyl and methylene protons, the NOE target function  $F_{\text{NOE}}$  was calculated using  $\langle r_c \rangle$  centre averaging with the same corrections of the upper limits of the target distances used in the equivalent pseudo-atom representation (Wüthrich *et al.*, 1983). An additional nine restraints were included for the three disulphide bonds present in crambin and CPI. (Note for each disulphide bridge there are three distance restraints,  $S_i-S_j$ ,  $S_i-C^{\beta}$ , and  $S_j-C^{\beta}$ , whose target values were set to  $2.02 \pm 0.02$ ,  $2.99 \pm 0.5$  and  $2.99 \pm 0.5$  Å respectively.) These disulphide bridge restraints are treated in exactly the same manner as the interproton distance restraints.

A total of 13 calculations were carried out for crambin, 10 for CPI and 10 for BSPI-2, differing in the values of the random number seed used for the assignment of the velocities at  $t = 0$  ps and for the partial rerandomization of velocities during the

course of the simulations. Nine of the crambin calculations, eight of the CPI ones and five of the BSPI-2 ones converged to similar final structures with an average backbone (N, C $\alpha$ , CO, O) atomic r.m.s. difference between them of  $2.2 \pm 0.3$ ,  $2.4 \pm 0.3$  and  $2.5 \pm 0.2$  Å respectively (Table I), all of which satisfied the experimental restraints within the errors specified (Table II). This success rate is comparable in our experience with that obtained for these proteins with the matrix distance geometry program DISGEO (Havel, 1986) and significantly higher than that obtained using the restrained molecular dynamics protocols used previously in our model crambin calculations (Clare *et al.*, 1986a; Brünger *et al.*, 1986; G.M. Clare, M. Nilges and A.T. Brünger, unpublished data). Typical computing times per simulation were  $\sim 1$  h for CPI,  $\sim 1.5$  h for crambin and  $\sim 4$  h for BSPI-2 on a CONVEX-C1XP computer. Plots of atomic r.m.s. difference as a function of residue number between



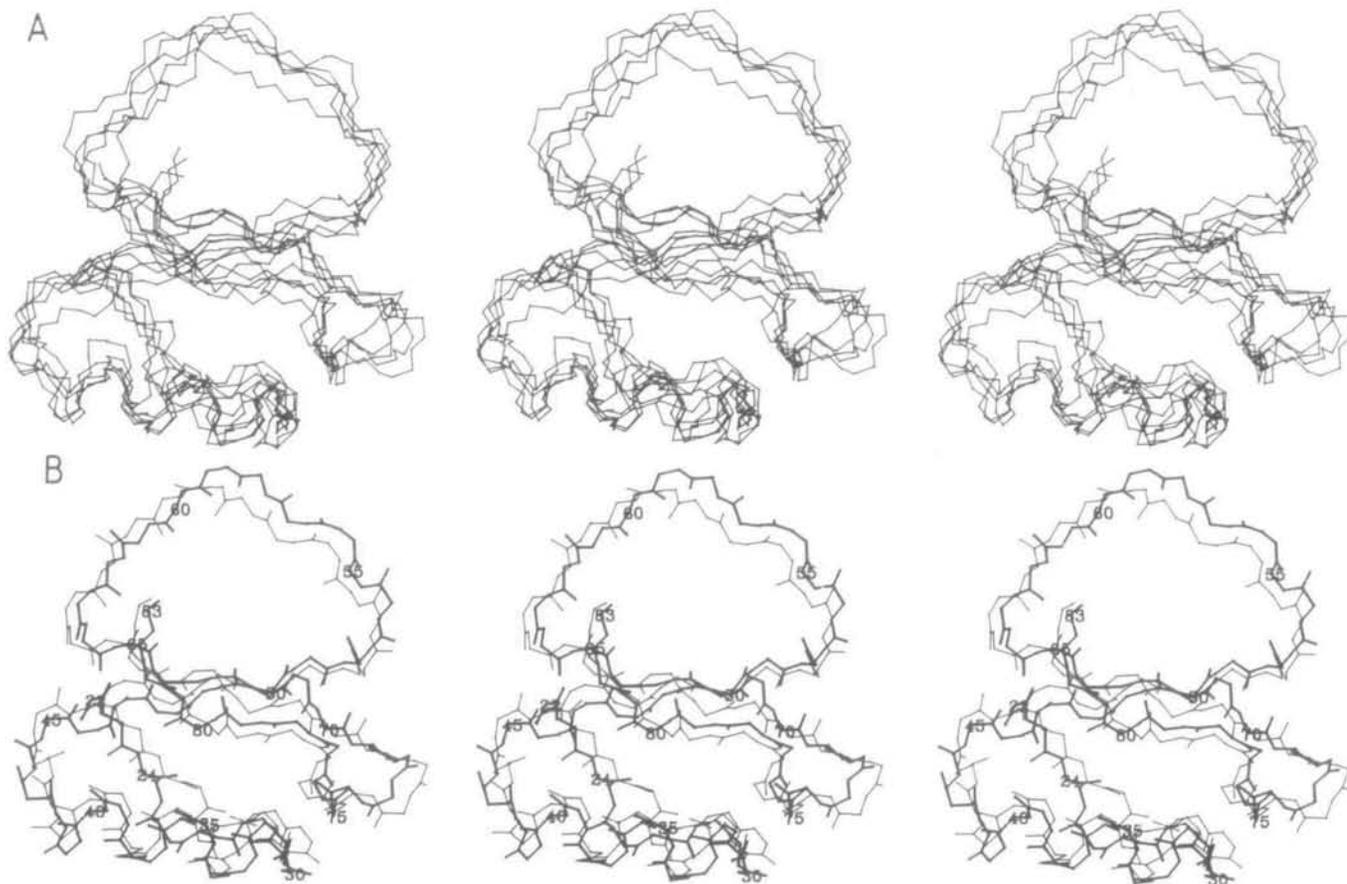
**Fig. 6.** (A) Best-fit superposition of the backbone (C, C $\alpha$ , N) atoms of the eight converged SA structures of CPI; (B) best-fit superposition (residues 2–38) of the backbone (C, C $\alpha$ , N, O) atoms of the (SA)r structure (thick lines) with the X-ray structure of CPI (thin lines). The three-picture stereo system used in this figure enables readers with both natural and cross-over stereo vision to view the images. For normal vision, select the left and centre images; for cross-over vision, use the centre and right images.

the individual converged  $\langle SA \rangle$  structures and the mean  $\overline{SA}$  structure derived by averaging their coordinates are shown in Figure 4, and stereoviews of best-fit superpositions of the converged  $\langle SA \rangle$  structures are shown in Figures 5–7.

From the atomic r.m.s. distribution of the  $\langle SA \rangle$  structures (Table I) it is clear that the size of the conformational space sampled by simulated annealing is comparable with that sampled by restrained molecular dynamics and slightly larger than that sampled by metric matrix distance geometry. Although all the simulated annealing calculations start off from the same initial structure, it must be emphasized that varying the random number seed used in the assignment of the initial velocities ensures that different convergence pathways are followed such that the different trajectories do not possess any common intermediate structures. That is to say that during the initial stages of the simulation the different trajectories diverge. In the case of the crambin trajectories the maximum average and maximum absolute backbone atomic r.m.s. differences are 5.4 and 8.1 Å respectively. As the simulation proceeds, and more and more NOEs are satisfied, so convergence between the different trajectories gradually occurs. This is illustrated in Figure 8. One cannot expect the trajectories, however, to diverge to the extent that the distribution of the structures between the different trajectories would be totally

random (with an expected mean backbone atomic r.m.s. difference of  $\sim 10$  Å for a protein the size of crambin; Cohen and Sternberg, 1980). The reason for this is twofold. First, local convergence, driven by the short-range NOEs, occurs from the beginning of the calculations. Second, the structures have a tendency to stay extended in the absence of tertiary folding forces (i.e. the long-range NOEs) due to their intrinsic inertia (arising from the fact that the masses of the atoms enter explicitly into the calculations; cf. equation 2). Nevertheless, we feel that this does not introduce any significant bias into the end result, particularly as misfolding can also occur, and in our view it is equivalent to using a set of randomly chosen initial structures in static real space methods (Braun and Go, 1985; Billeter *et al.*, 1987).

The non-bonded contacts in the converged structures are all good, as evidenced by negative values for van der Waals energy calculated using the CHARMM empirical energy function (Table II). Indeed they are comparable with those of the restrained molecular dynamics structures. Thus, our choice of a final van der Waals radius, a factor of 0.8 smaller than the one used to compute the Lennard–Jones van der Waals energy, is completely reasonable. Further, these results suggest that the converged  $\langle SA \rangle$  structures do not require any further refinement by restrained molecular dynamics. In this respect, we note that the



**Fig. 7.** (A) Best-fit superposition (residues 22–83) of the backbone (C, C $\alpha$ , N) atoms of the five converged SA structures of BSPI-2; (B) best-fit superposition (residues 22–83) of the backbone (C, C $\alpha$ , N, O) atoms of the (SA)r structure (thick lines) with the X-ray structure of BSPI-2 (thin lines). The three-picture stereo system used in this figure enables readers with both natural and cross-over stereo vision to view the images. For normal vision, select the left and centre images; for cross-over vision, use the centre and right images.

non-bonded contacts in the metric matrix distance geometry structures are considerably poorer, insofar as the van der Waals energies tend to be large and positive, and are only improved by additional restrained molecular dynamics refinement.

The converged <SA> structures are all reasonably close to the respective X-ray structures with an average backbone atomic r.m.s. difference of 2–2.5 Å (Table I). Averaging the structures results in mean structures that are close to their respective X-ray structure than any of the individual <SA> structures. The same is true of the metric matrix distance geometry and restrained molecular dynamics structures. Interestingly, the r.m.s. differences between the mean structures calculated by the three different methods are comparable with the difference between the individual mean structures and the X-ray structures. The average SA structures are clearly very bad both with respect to stereochemistry and non-bonded contacts (Table II). These are easily corrected by 1000 cycles of Powell restrained minimization with only minor accompanying atomic r.m.s. shifts to generate the structures (SA)r (see Table I). In this procedure the restraints force constant  $k_f$  for the final NOE potential  $F_{\text{NOE}}$  is kept constant at 60 kcal/mol/Å<sup>2</sup>, the force constant  $k_r$  for  $F_{\text{repel}}$  is multiplied by two every 20 cycles from an initial value of 0.2 kcal/mol/Å<sup>2</sup> to a maximum value of 4 kcal/mol/Å<sup>2</sup>, and the hard-sphere van der Waals radii are kept constant at 0.8 times their Lennard–Jones values. Best-fit superpositions of the (SA)r and X-ray structures are shown in Figures 5 (crambin), 6 (CPI) and 7 (BSPI-2).

Examination of the radii of gyration indicates that the <SA> structures, like the distance geometry structures, tend to be a little expanded relative to the X-ray structure, whereas the restrained dynamics structures tend to be compressed (Table II). This is due to the different representation of the van der Waals interactions used in the different methods (i.e. simple repulsion terms in the case of the simulated annealing and distance geometry calculations compared with a full Lennard–Jones potential with an attractive component in the case of the restrained molecular dynamics calculations).

### Concluding remarks

In this paper we have shown that simulated annealing is an effective method of determining three-dimensional structures on the basis of interproton distance data. The present calculations indicate that it is comparable in speed with distance geometry calculations and significantly faster than restrained molecular dynamics calculations employing a full empirical energy function. This is largely due to the replacement of the non-bonded interaction potentials in the empirical energy function by a simple van der Waals repulsion term. In addition, the agreement with the experimental interproton distance restraints and the quality of the non-bonded contacts exhibited by the converged SA structures is comparable with that of structures obtained or refined by restrained molecular dynamics and significantly better than that of structures obtained by metric matrix distance geometry calculations alone (see Table II). Critical to the success of the

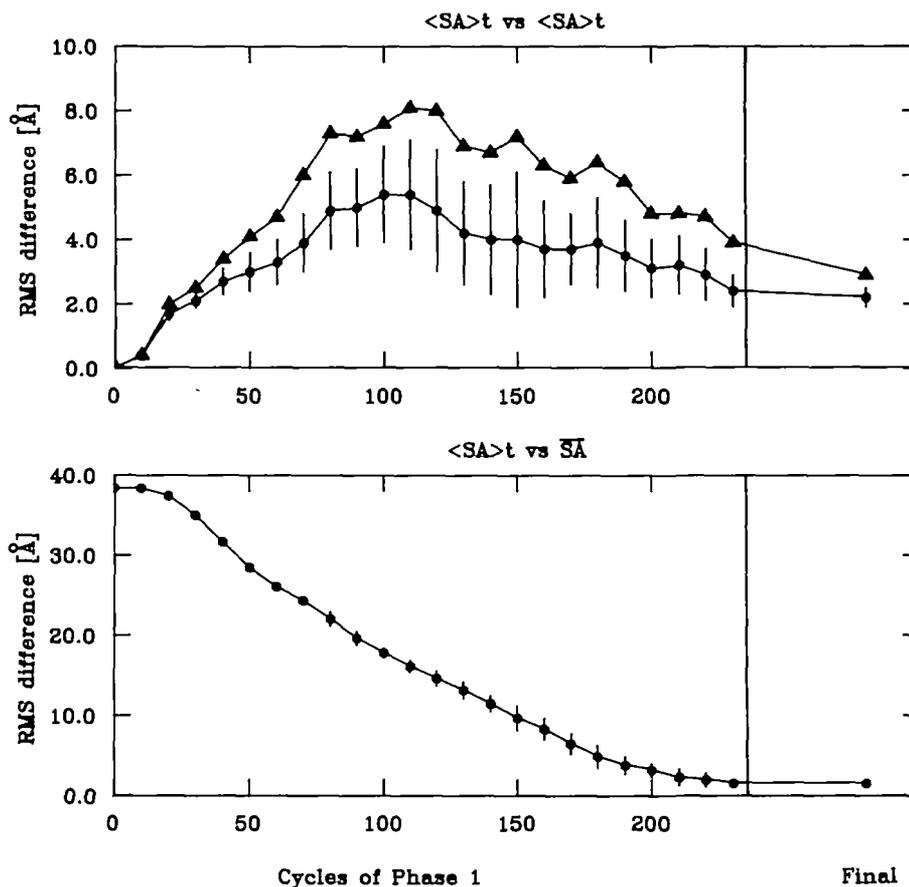


Fig. 8. The convergence pathways for the nine crambin trajectories. (A) Plot of the average (●) and maximum (▲) backbone atomic r.m.s. difference between the different trajectories as a function of time. (B) Plot of the average r.m.s. difference between the structures of the different trajectories on the one hand and the final average structure SA on the other, as a function of time. Each cycle of annealing corresponds to a time of 40 fs and 250 cycles corresponds to 10 ps. The bars represent the standard deviations in the average values.

method is the protocol employed, in particular the way in which the NOE distances are partitioned between different functional forms.

At this stage we would not claim that the radius of convergence of the simulated annealing method is any larger than that of the various methods already published. Nevertheless, it forms a useful addition to the arsenal of tools available to the NMR spectroscopist interested in solving three-dimensional structures of proteins. This is particularly so as the convergence properties of the various methods are likely to be dependent on both the nature of the structure being solved and the extent of the experimental data at hand.

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