Measurement of Homonuclear Proton Couplings from Regular 2D COSY Spectra

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DEDICATED TO PROFESSOR RAY FREEMAN ON THE OCCASION OF HIS 67TH BIRTHDAY

Received November 17, 2000; revised January 11, 2001; published online March 21, 2001

An interactive computer procedure is described which determines ¹H-¹H couplings from fitting the cross-peak multiplets in regular phase-sensitive COSY spectra. The robustness and simplicity of the method rely on the fact that a given cross-peak intensity is not an independent variable in the fitting procedure, making it possible to measure couplings accurately even from individual cross peaks with unresolved multiplet structure.

INTRODUCTION

 $^{1}\text{H}^{-1}\text{H}$ J couplings provide important dihedral information, which is widely used during NMR structure determination. Numerous methods have been proposed for measuring such couplings, primarily aimed at cases where the ¹H multiplet is too overlapped or broad in the 1D spectrum to yield resolvable splittings. These include homonuclear J spectroscopy (1), homonuclear E.COSY methods (2), heteronuclear E.COSY (3), triple-resonance E.COSY (4), quantitative J correlation (5, 6), comparison of cross sections through in-phase and antiphase cross peaks (7, 8), and the so-called DISCO method (9), which relies on the same principle. Two new quantitative J correlation methods, based on constant-time COSY, can also yield useful information (10, 11). None of these approaches is fully satisfactory, however, when working with macromolecules at natural abundance, particularly when cross peaks do not exhibit fine structure and most diagonal multiplets overlap one another.

Here, we describe a simple but effective method to directly obtain quantitative *J*-coupling information from cross peaks in regular phase-sensitive COSY spectra by amplitude-constrained multiplet evaluation (ACME). Problems with deriving *J* splittings from antiphase COSY spectra have long been recognized (12-14) and relate to the fact that the antiphase peak-to-peak splitting in a COSY-type spectrum is a function of both the linewidth and the magnitude of the passive and active *J* couplings. Some methods derive the *J* couplings from least squares fitting of a cross peak to a convolution of an antiphase and several in-phase splittings, using the intensity of the cross peak

as a variable, nonconstrained parameter in the fit. However, an increase in linewidth results in a larger antiphase separation of lower intensity for the cross peaks, whereas an increase in active unresolved J coupling results in a similar increase in antiphase splitting but larger cross-peak intensity. Without constraining the amplitude of the cross peak, this makes it difficult to separate the effects of linewidth and active coupling, resulting in poorly determined J values. Inherently better algorithms fit either a group of multiplets or the entire NMR spectrum simultaneously (15-18). These algorithms implicitly use the fact that all fitted multiplets have the same intrinsic intensity (i.e., the same integrated intensity if all splittings were in-phase). The effectiveness of these methods is due to the fact that active coupling values in one multiplet appear as passive couplings in related multiplets. Typically, such methods require extensive definitions of the spin topologies and chemical shift assignments of all related multiplets and may require some degree of multiplet fine structure. Furthermore, because of the potentially large numbers of spectral parameters to be fit, these methods usually require prior knowledge or tight constraints for many spectral parameters in order to make optimization tenable. This has so far limited the application of these methods.

Here, we demonstrate that by simply constraining the multiplet intensity, the ACME method makes it possible to extract couplings accurately and conveniently by fitting individual multiplets or small clusters of overlapping multiplets, without the need to consider all related multiplets simultaneously. To establish the multiplet intensity constraint, we use the information that the intrinsic intensity of all multiplets in the spectrum is the same and identical to that of the in-phase diagonal multiplets for the case where a 90° mixing pulse is used. This procedure is very simple from a user perspective and circumvents the convergence problem, while retaining a sharp and accurate minimum for the fitted active J coupling. This method does not require fine structure for the antiphase multiplets that need to be fitted and therefore is also ideally suited to fitting the very complex unresolvable multiplets that are typically obtained in COSY spectra of macromolecules weakly oriented in a liquid crystalline phase. Ignoring cross-correlated transverse relaxation, and assuming the weak coupling limit, the time domain signal of the A-spin diagonal, $S_{AA}(t_1, t_2)$, and AX cross peak, $S_{AX}(t_1, t_2)$, in a COSY experiment are given by

$$S_{AA}(t_1, t_2) = S_0 \Pi_k \cos(\pi J_{Ak} t_1) \cos(\Omega_A t_1) \exp(-t_1/T_{2A})$$
$$\times \Pi_k \cos(\pi J_{Ak} t_2) \exp(i\Omega_A t_2) \exp(-t_2/T_{2A})$$
[1a]

$$S_{AX}(t_1, t_2) = S_0 \sin(\pi J_{AX}t_1) \Pi_{k \neq X} \cos(\pi J_{Ak}t_1) \cos(\Omega_A t_1)$$

$$\times \exp(-t_1/T_{2A}) \sin(\pi J_{AX}t_2) \Pi_{q \neq A} \cos(\pi J_{Xq}t_2)$$

$$\times \exp(i\Omega_X t_2) \exp(-t_2/T_{2X}), \qquad [1b]$$

where the products extend over all spins k coupled to A and spins q coupled to X, Ω_A and Ω_X are angular chemical shifts of spins A and X, and T_{2A} and T_{2X} are the A- and X-spin transverse relaxation times. It is clear from Eq. [1b] that the initial cross-peak "buildup" in the (t_1, t_2) time domain is simply $S_0 \sin(\pi J_{AX}t_1) \sin(\pi J_{AX}t_2) \approx S_0 \pi^2 J_{AX}^2 t_1 t_2$. So, if S_0 is known, the buildup of the time domain A-X cross-peak signal, which simply can be obtained by inverse Fourier transformation of a resolved cross-peak multiplet, provides a unique value for J_{AX} , with effects from passive couplings and T_2 only occurring at later times. As a result, J_{AX} is a nearly orthogonal variable relative to both the passive couplings and T_2 , but parallel to S_0 . It is therefore critical that an accurate value for S_0 is obtained prior to fitting the cross peaks. If the delay between scans is sufficiently long, the same S_0 value applies for all multiplets within a given molecule and can be obtained from the initial $(t_1 = t_2 = 0)$ time domain amplitude of either a diagonal multiplet (Eq. [1b]) or the entire normalized time domain signal. The need for constraining the amplitude (scale factor) in the fit has been mentioned before (15-18), but was less critical in the application to fitting of the fine structure of multiple related multiplets of a given spin system. So, the main difference relative to earlier fitting procedures is that in ACME fitting the intrinsic signal intensity, S_0 , is held constant for all multiplets in the spectrum at a value determined experimentally from the diagonal (see below), and fine structure of the multiplet is not required for accurate measurement of a coupling. In contrast to most other fitting procedures, only the fitted value for the active coupling is meaningful. Fitted passive couplings and decay rates are parallel variables in parameter space and their optimum values generally do not provide useful coupling information. In practice, the actual fit is carried out in the frequency domain, using multiplet models generated by numerical Fourier transformation of the model time domain forms of Eq. [1]. The numerical Fourier processing of the model function is performed automatically during the fit according to the zero filling and window functions that were applied to the experimental data.

The fitting procedure has been implemented via a graphical interface constructed using NMRWish (19), a companion package to the NMRPipe processing and analysis system (20). NMRWish is a version of the Tcl/Tk script interpreter "wish" (21, 22), which has been augmented to include facilities for spectral display and manipulation, as well as relational database functions for manipulating spectral parameters, molecular structures, etc. Use of the graphical interface to extract couplings typically involves the following steps:

1. A cluster of one or more multiplets is selected interactively from a spectral display, and an expanded view of the selected region is shown.

2. The approximate center of each multiplet in the selected region is defined by manually positioning a cursor. Since the exact position of the multiplet center can be adjusted during the fit, its initial location is not critical.

3. An interactive parameter page is shown for each signal and is used to specify the parameters to be included in the signal description, the initial values of variable parameters, and values that are held constant during the fit. For example, one may specify how many passive couplings will be included in each dimension of the multiplet and rough estimates for their initial values. In order to accommodate signals from equivalent spins, such as CH₃ groups, more easily, one can also specify an integer intensity scaling factor for the number of equivalent superimposed signals or an integer exponent to a given modulation term for the number of equivalent couplings. As these passive couplings and decay rates are orthogonal in parameter space relative to the active coupling, their initial values are not critical and only become relevant when a cross peak displays fine structure, i.e., more than four components per multiplet.

4. Once the parameters of the signal models are defined, the fit is performed. In most cases, the signal positions, widths, and couplings are all allowed to vary, and only the intensity is held constant. The final multiplet model and residual are then displayed along with the experimental region, and the values shown in the parameter pages are updated to reflect the results of the fit.

5. The results are evaluated, either according to their χ^2 value or, for cases where not all signals in the selected region are included in the model, by inspection of the residual spectrum. If inspection of the results indicates that the model is reasonable, the fit is accepted and the results are automatically recorded in a table. If assignments are available, these can be entered and recorded along with the coupling values.

The fitting procedure itself is currently implemented via a macro interpreter that generates the model function at each iteration. This allows for substantial flexibility, for example, by making it straightforward to adjust the model to account for dephasing delays inserted prior to the acquisition or to extend the method to 3D data. However, use of an interpreted fitting function makes this implementation relatively slow, with computation times of several seconds for fitting a single multiplet and a minute or more for complicated clusters of multiplets. Nevertheless, this is still fast enough for the method to be convenient, especially in light of the fact that no complicated definition or setup is required in order to extract couplings. More information is provided at http://spin.niddk.nih.gov/bax/NMRPipe/cosy.

Prior to fitting the cross peaks, it is useful to remove the diagonal signals, which as a result of their long dispersive tails can interfere with the cross peaks. This can simply be done by subtracting the diagonal region of the COSY spectrum where the diagonal is phased to be absorptive, followed by Hilbert transformation and rephasing to make the cross peaks absorptive (23). An alternative method for doing this, which has the additional advantage of avoiding discontinuities near the edge of the cutout diagonal region, has been implemented in the NMR-Pipe processing software. This procedure works by temporarily shifting the diagonal to the center of the spectrum so that it can be removed by traditional numerical solvent suppression methods (24). A variation on this scheme can be used to produce a complementary spectrum that contains only the absorptive diagonal signals. A complete description of these processing schemes, along with example NMRPipe processing scripts, can be found at http://spin.niddk.nih/bax/NMRPipe/diag.

An example of part of the COSY spectrum of human ubiquitin, from which the diagonal has been removed in the above manner, is shown in Fig. 1. A second spectrum containing only the absorptive diagonal signals is also derived (not shown). Fit-



FIG. 1. Region of the 800-MHz phase-sensitive COSY spectrum of human ubiquitin (1.5 mM, pH 6.8, 10 mM phosphate uncorrected meter reading), recorded in D₂O, from which the dispersive diagonal signals have been removed using the procedure described in the text. The spectrum was acquired as a $512^* \times 2048^*$ data matrix with identical spectral widths (9 kHz) in the two dimensions. Data were apodized with 90°-shifted sine bell (t_1) and 90°-shifted squared sine bell (t_2) windows, prior to zero filling to 2048* × 4096*.



FIG. 2. The H^{β}-H^{α} cross peak of ubiquitin Lys⁶ in the 800-MHz COSY spectrum. (A) experimental data, (B) best fit simulated data using the correct intensity factor (*I* = 1), and best fits when the intensity was constrained to be 10-fold (C) or 100-fold (D) larger. Note that the goodness of the fit (χ^2) is essentially the same for the three simulated spectra.

ting of a single isolated, in-phase diagonal multiplet is rather insensitive to initial linewidth or multiplicity and can be used to obtain the intrinsic signal amplitude. This fit can be repeated for several diagonal signals in order to establish reproducibility. In the ubiquitin case, fitting six different diagonal signals indicates that the amplitude could be determined to an accuracy of better than 5%. Alternatively, the integrated intensity of the entire diagonal subspectrum, or a fraction thereof, divided by the number of spins contributing to this diagonal can be used.

Figure 2 shows how the best-fit active J coupling for the ubiquitin Lys⁶ H^{β''}-H^{α} COSY cross peak depends strongly on this intrinsic intensity. Figure 2A is the experimental multiplet, whereas Figs. 2B-2D are best-fitted simulated multiplets, where the intrinsic amplitude has been set at its true value (Fig. 2B) and at 10 and 100 times larger values (Figs. 2C and 2D). The goodness of the fit (χ^2) for the multiplet shown is nearly indistinguishable, yet the magnitude of the active coupling decreases by almost an order of magnitude when the intrinsic intensity, *I*, is increased from 1 to 100. To a good approximation, in the limit where the linewidth is larger than the active J coupling, the best fitted coupling scales with the square root of the intensity, whereas the goodness of the fit remains comparable (Fig. 2). This confirms that in the absence of amplitude information it is not possible to obtain an accurate J coupling from fitting a single antiphase COSY cross peak.

So, passive couplings can be kept either as fixed or as adjustable parameters during the fitting procedure. If kept variable, the accuracy of the resulting best fitted *passive* couplings is poor, however, as the effect of an unresolved passive coupling is similar to that of the fitted natural line width parameter. Convergence of the least-squares minimizer is fastest when estimated approximate values for the passive couplings are entered as fixed nonvariable parameters. This is typically the method in which we use the fitting procedure when no (partially) resolved passive splittings are observed in the cross peak.

The graphical interface for coupling extraction is shown in Fig. 3. The window in Fig. 3A shows a small region of the COSY spectrum of ubiquitin. The boxed region shows the group of multiplets manually selected for analysis. The window in Fig. 3B contains the parameters of a fitted model for the first of five interactively selected signals. Parameters that are variable during the fit are marked by black checkboxes. The selected spectral

region, corresponding model, and residual spectrum are shown together in a third window (Figs. 3C, 3D, and 3E). If multiple identical passive couplings are present, as, for example, in the case of the three $H^{\beta}-H^{\gamma}$ couplings in a $H^{\beta}-H^{\alpha}$ cross peak of threonine residues, the multiplicity for a single passive coupling can be set to "3" in the parameter window, rather than defining three independent couplings. Similarly, when fitting a cross peak involving a methyl group, the intensity can be multiplied by 3. The user interface currently allows for up to five multiplets with up to three independent passive couplings per dimension to be fit simultaneously. For larger numbers of cross peaks, the accuracy and convergence of fitted parameters decrease. As shown



FIG. 3. Graphical interface for coupling extraction. (A) Region of the COSY spectrum with a zoom box marking the spectral region on which multiplet fitting is to take place. (B) Parameter window that defines adjustable (dark checked box) and fixed parameters to be used in the fit for the first of up to five cross peaks. For passive couplings, the "A¹" mark indicates the number of passive couplings of this size to be included in the simulation, i.e., for passive coupling to a methyl group this value is changed to "A³." Similarly, the intensity parameter "Hi^{*}1" can be adjusted to "Hi^{*}3" for cross peaks involving a methyl group. Experimental data (C), best fitted data (D), and difference spectrum (E) when only the signals of the five rightmost cross peaks are entered in the parameter window and included in the fit optimization. The nonzero residuals seen in (E) result primarily from neglect of non-first-order effects and inhomogeneity broadening in the model function.



FIG. 4. Comparison of 58 ${}^{3}J(H^{\alpha}, H^{\beta})$ couplings in human ubiquitin, measured with the new fitting procedure (vertical axis) versus those measured previously with the HA(CA)HB experiment. The systematically smaller value for the HA(CA)HB derived couplings is attributed to the effect of passive spin-flips, which do not affect the result of the ACME fit.

in Fig. 3, not all cross peaks present in the selected window region (Fig. 3C) need to be included in the fit. To illustrate this feature, only five of the eight cross peaks present in Fig. 3C were included, and the additional cross peaks remain present in the difference spectrum (Fig. 3E).

When fitting spectra recorded in a dilute liquid crystalline phase (25), frequently the number of passive couplings will be much larger than 3. However, from a practical perspective, only the largest passive couplings play a role in the fitting procedure and three passive couplings are more than sufficient for the wide variety of spin systems we have studied so far.

Figure 4 compares values for all 58 ${}^{3}J(\mathrm{H}^{\alpha},\mathrm{H}^{\beta})$ couplings previously measured with the HA(CA)HB experiment (6) with those obtained from the new fitting procedure. On average, Jvalues derived from the HA(CA)HB spectrum underestimate the true coupling if no correction is made for the finite life time of the spin state of the coupling partner (6). Because the new fitting procedure is not affected by spin-flips of the passive spin, which merely affect the fitted linewidth, fitted J values tend to be larger. Overall, agreement is good (Pearson's correlation coefficient R = 0.93) and comparable in quality to that between HA(CA)HB data and heteronuclear E.COSY measurements for ubiquitin (data not shown). This indicates that the present approach for measuring these couplings is equally robust and therefore quite accurate. Any given coupling can be measured twice, from each of the two corresponding cross peaks. Reproducibility is invariably found to be quite high, with a root-mean-square difference of 0.7 Hz over the entire set of H^{α}/H^{β} cross peaks (N = 78), indicating a random uncertainty of ± 0.5 Hz in individual fits.

One detail that may require particular attention is the assumption of uniform intrinsic intensity. In order for this assumption

to be valid, the spin system must be fully relaxed at the start of the COSY pulse sequence. Alternatively, two spectra with different interscan delays may be used, such that incomplete T_1 relaxation rates can be accounted for. Also, water suppression in phase-sensitive COSY spectra can be a problem as solvent presaturation may unevenly affect the longitudinal ¹H magnetization through spin diffusion involving spatially proximate exchangeable protons or protons resonating in the immediate vicinity of the H₂O signal. For this reason, we prefer to record the COSY spectrum in D₂O. In principle, double quantum filtering may also be used to attenuate the H_2O signal (26). However, this decreases the inherent sensitivity of the COSY experiment twofold and does not solve the dynamic range problem because the water signal remains present in individual transients. Also, it removes the amplitude information contained in the diagonal and therefore makes our fitting procedure less straightforward. In nucleic acids, partial exchange of base protons with solvent deuterons can result in erroneous amplitudes and thereby introduce errors in the derived couplings. The same, of course, applies to cross peaks to amides for proteins dissolved in D₂O or the partial attenuation when dissolved in 90% H₂O/10% D₂O.

The fitting procedure is based on the use of Eq. [1], i.e., on the assumption of first-order, weakly coupled spectra. Fitting of cross peaks very close to the diagonal is affected by the diagonal removal routine described above and therefore does not yield reliable results. However, for the common case where A-X and B-X couplings need to be measured in a moderately strongly coupled ABX system, with $|\delta_A - \delta_B| > \sim 5|J_{AB}|$, ACME fitting of simulated spectra reproduces the A-X and B-X couplings very well. The remarkable robustness of the fitting procedure to non-first-order effects is related to the fact that the initial buildup rate of the integrated A-X cross peak intensity in the ABX spin system is little affected by the strong coupling, even though the χ^2 is considerably higher. Clearly, a more rigorous approach would be to include the effects of strong coupling in the model function (18). However, this would make use of the ACME fitting more complex because complete definition of each spin system would be required prior to the fit and has not yet been implemented.

The ACME program contains the option to include the effect of delays preceding the t_1 and/or t_2 evolution period. Such delays may be desirable to allow dephasing of the rapidly decaying signals of bicelle or phage liquid crystal contributions.

The method described here is particularly useful for measurement of ${}^{1}H{-}^{1}H$ couplings in molecules that are weakly aligned in a dilute liquid crystalline phase. These frequently give rise to completely unresolvable cross-peak multiplets with more than half a dozen passive couplings that are difficult to analyze accurately using the E.COSY method. The principal disadvantage of the ACME method is the absence of sign information for the coupling involved. Several novel heteronuclear E.COSY-like methods have been presented recently that permit experimental measurement of both the sign and the magnitude of ${}^{1}H{-}^{1}H$ couplings (27, 28). However, without isotopic enrichment, such experiments are generally not applicable to macromolecules. If a reasonably accurate initial structure is available, this frequently can be used to determine the sign of the coupling. Alternatively, the structure calculation can use the absolute values of ${}^{1}\text{H}{-}{}^{1}\text{H}$ dipolar couplings as input restraints (29).

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